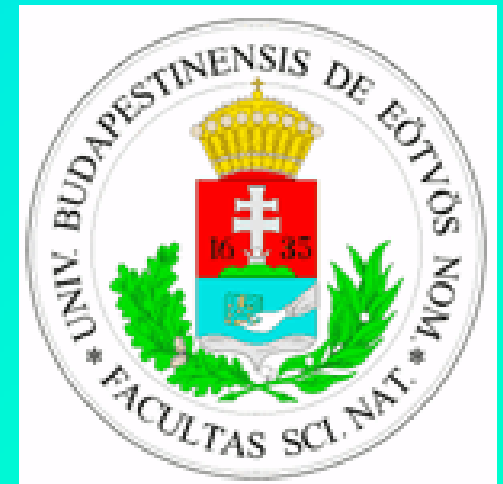


**Cserti József**

# **A nanofizika új eredményei**

**Eötvös Loránd Tudományegyetem  
Komplex Rendszerek Fizikája Tanszék**

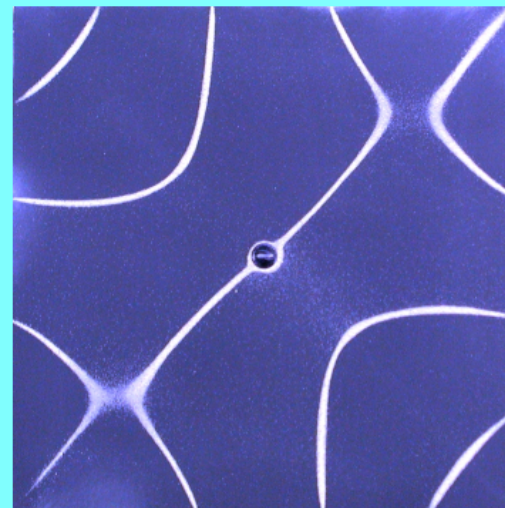
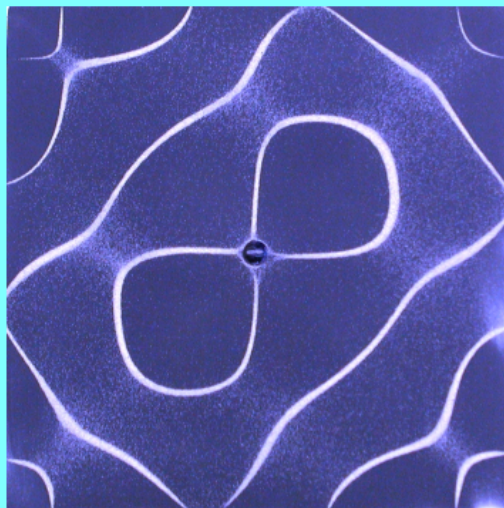
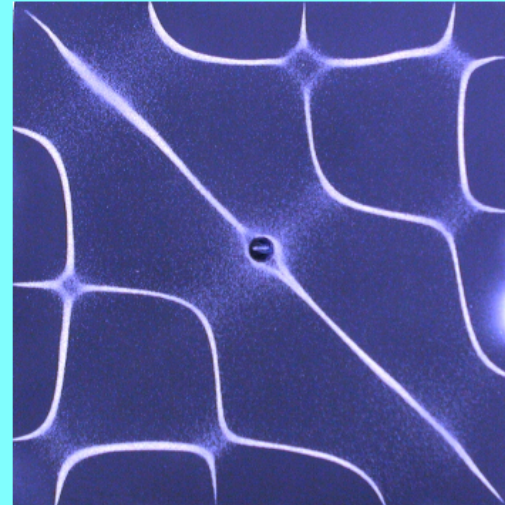
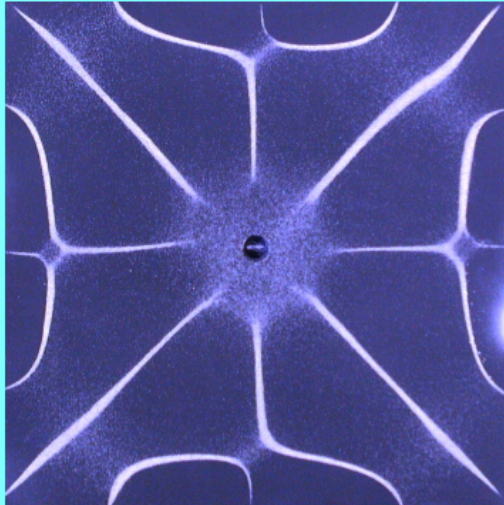


Az atomtól a csillagokig, 2006. április 27.

# Chladni lemezek



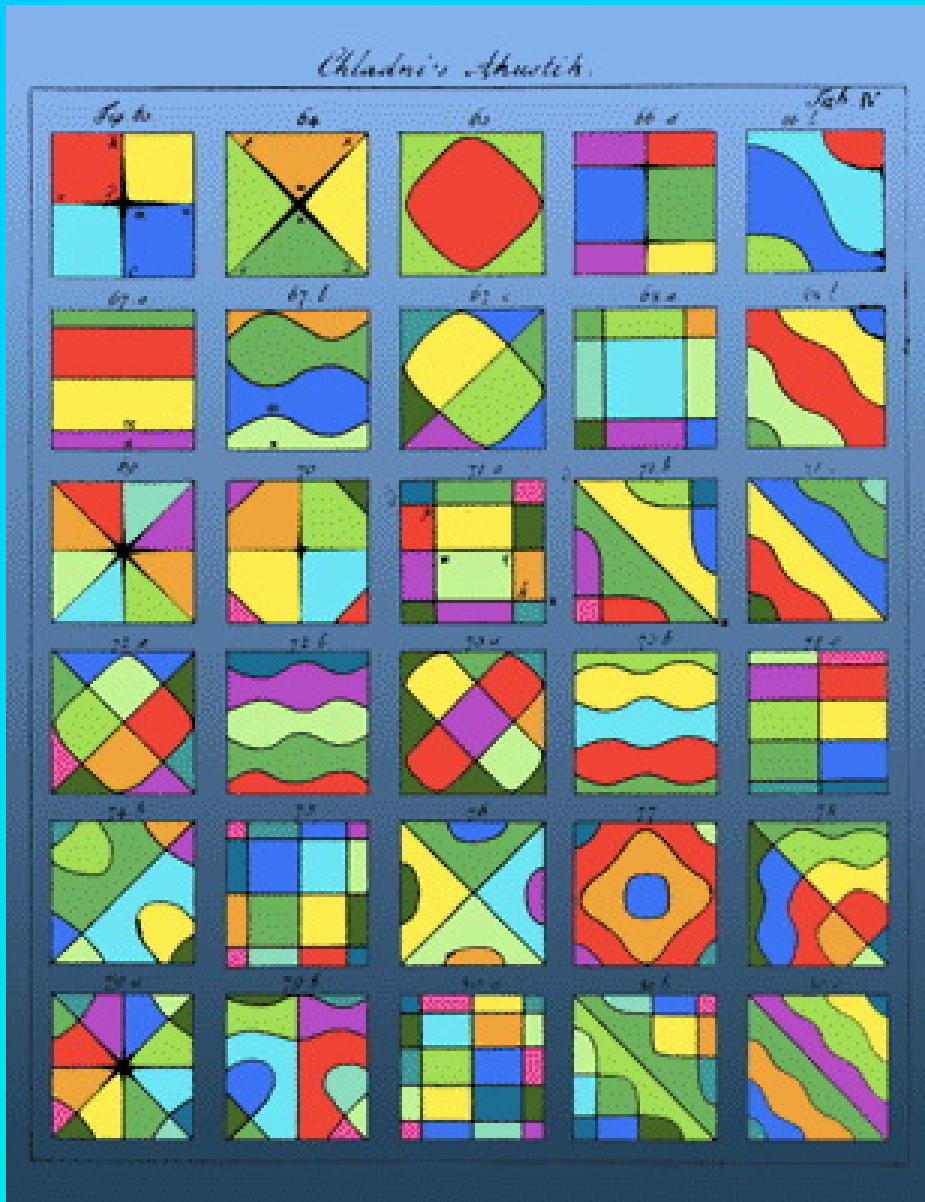
Bérces György  
Eötvös Loránd Tudományegyetem  
Anyagfizikai Tanszék

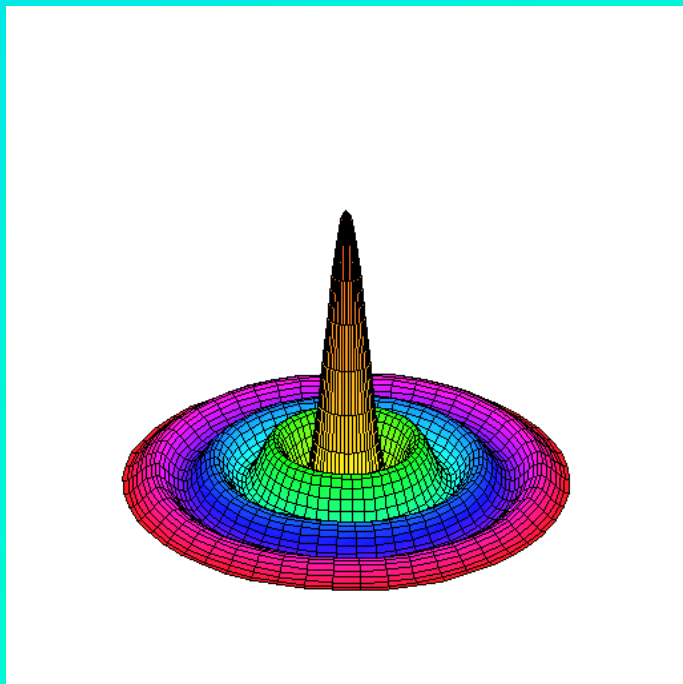
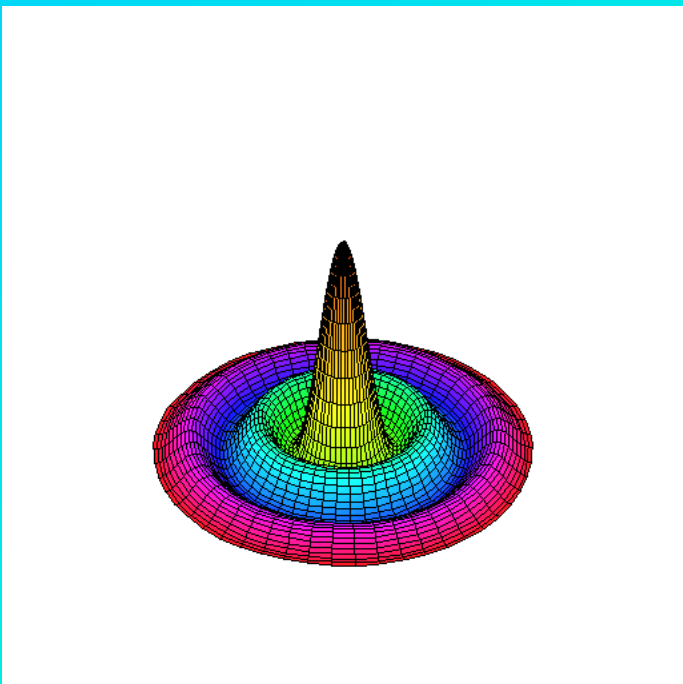
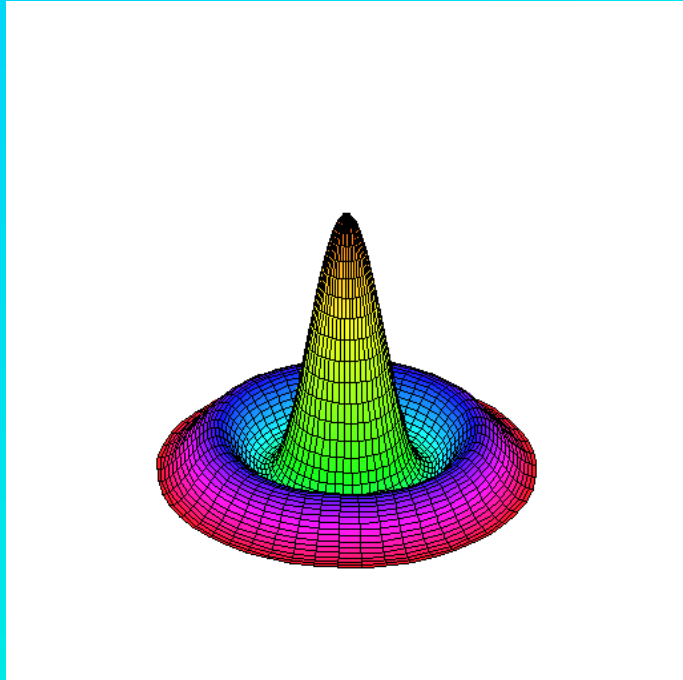
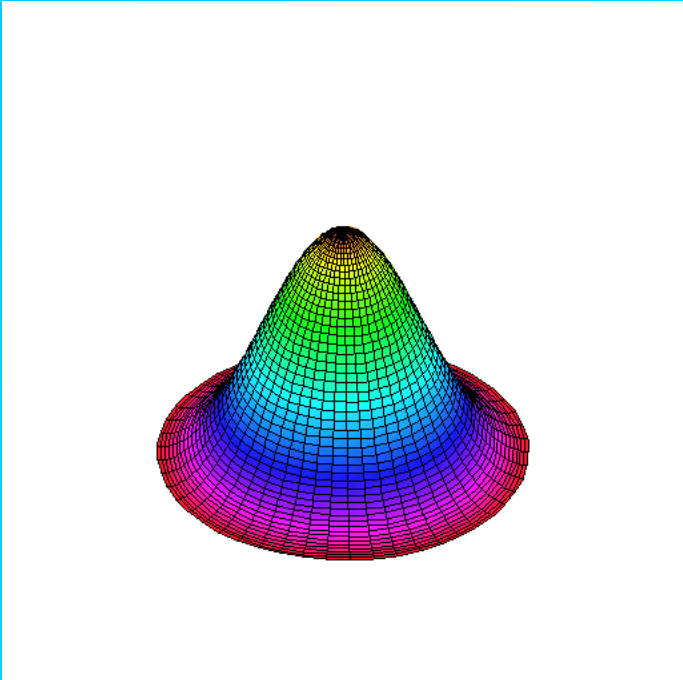


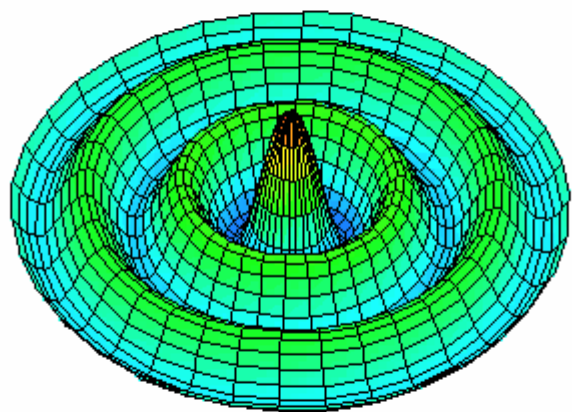


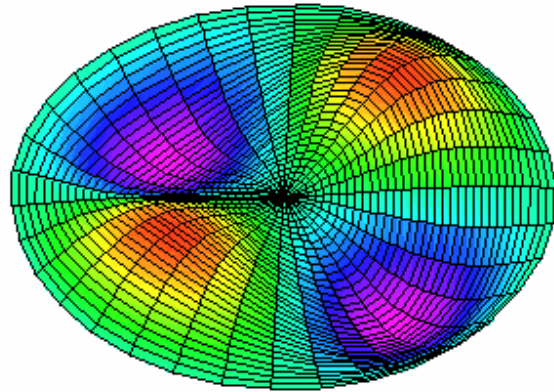


# Ernest Florens Friedrich Chladni (1756 - 1827)

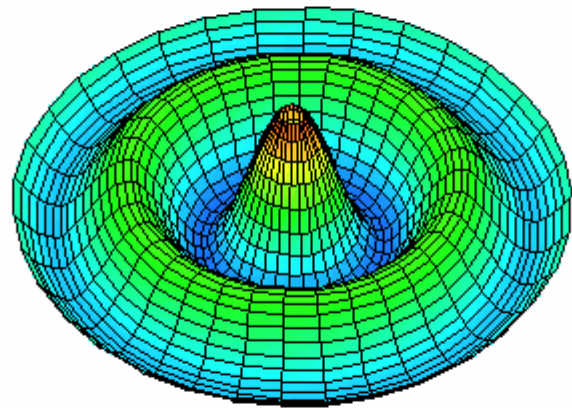


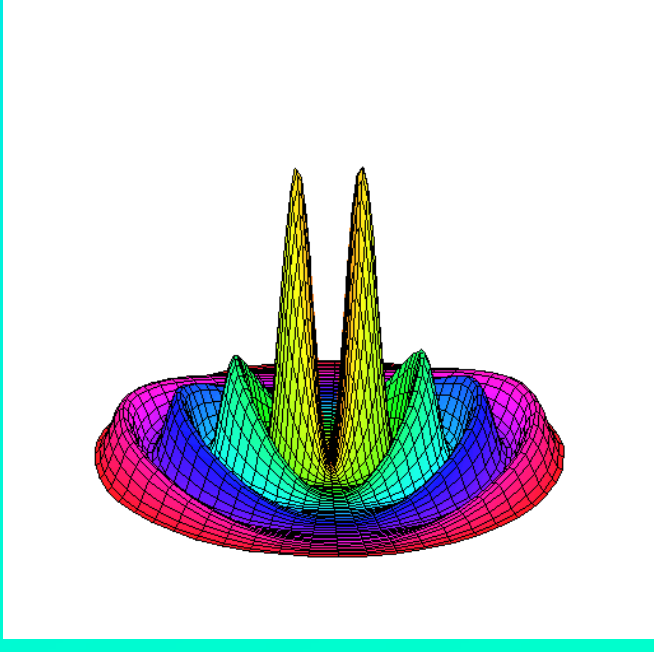
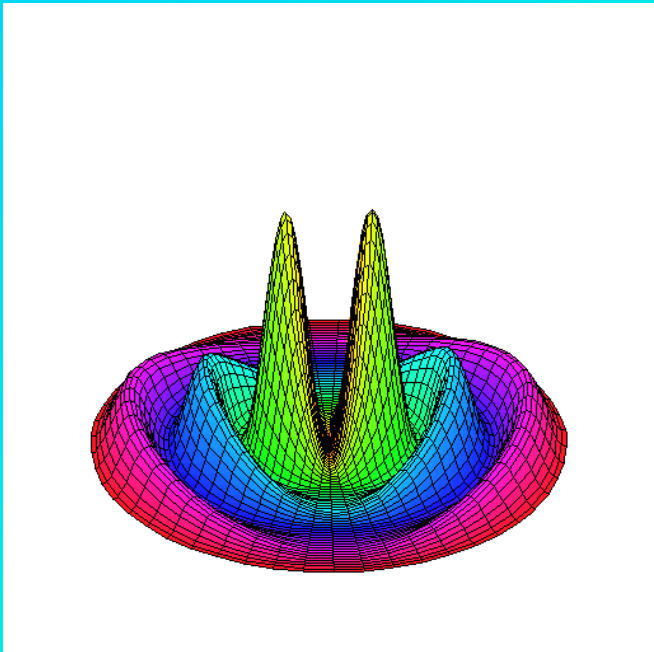
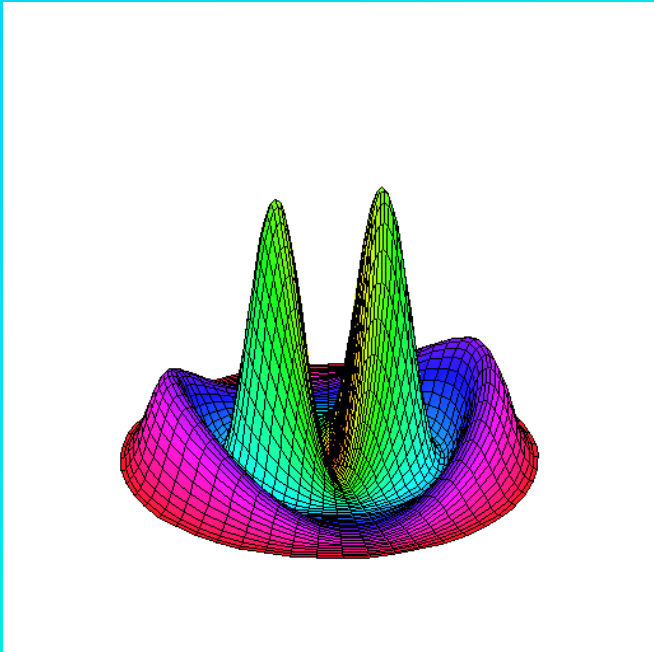
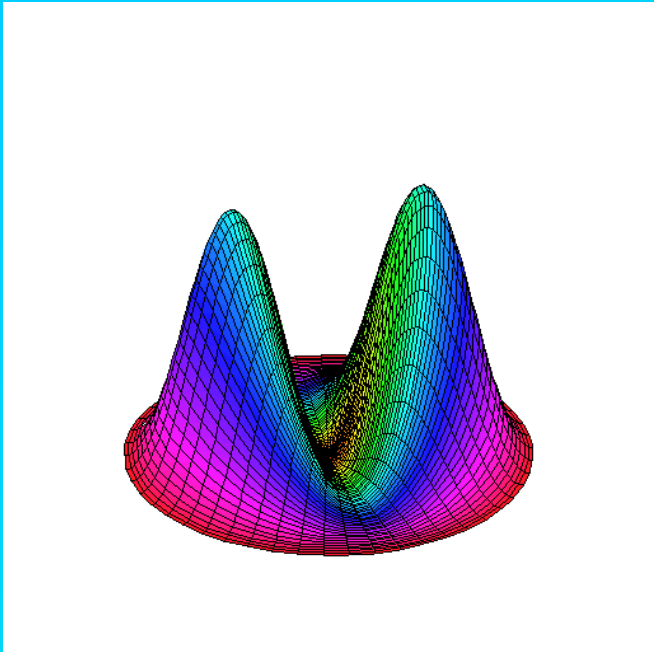


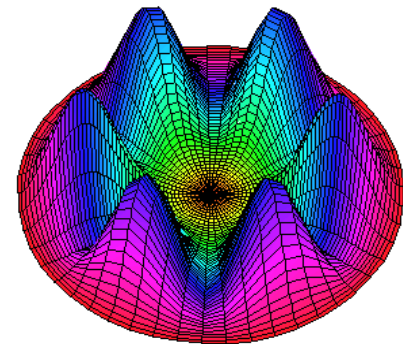
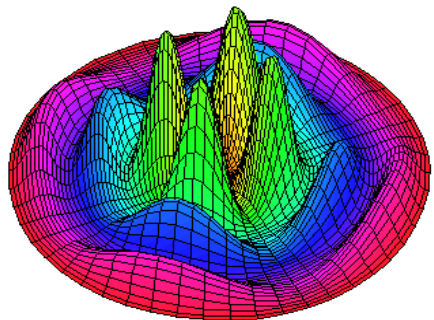
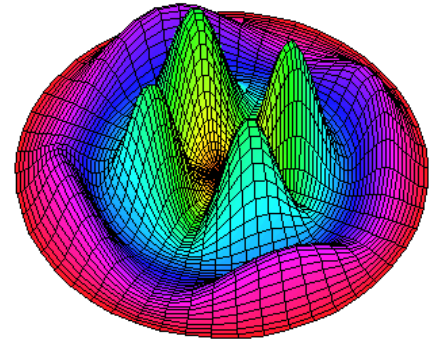
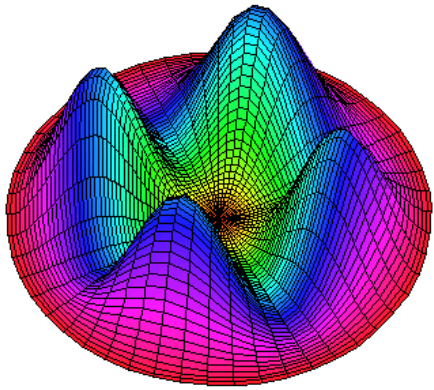




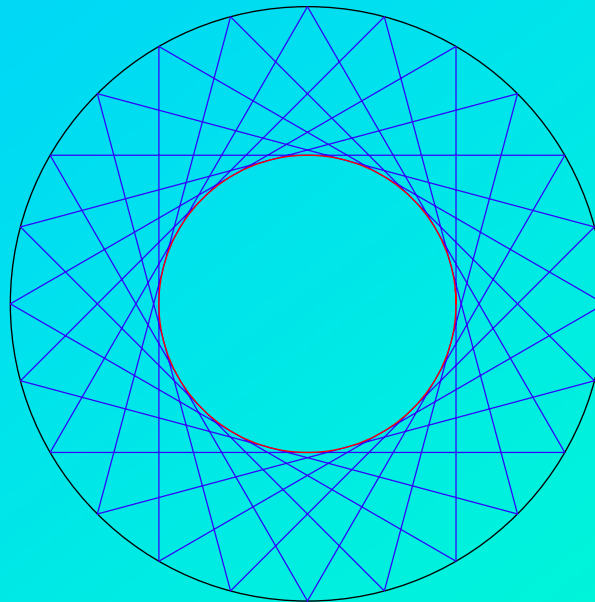






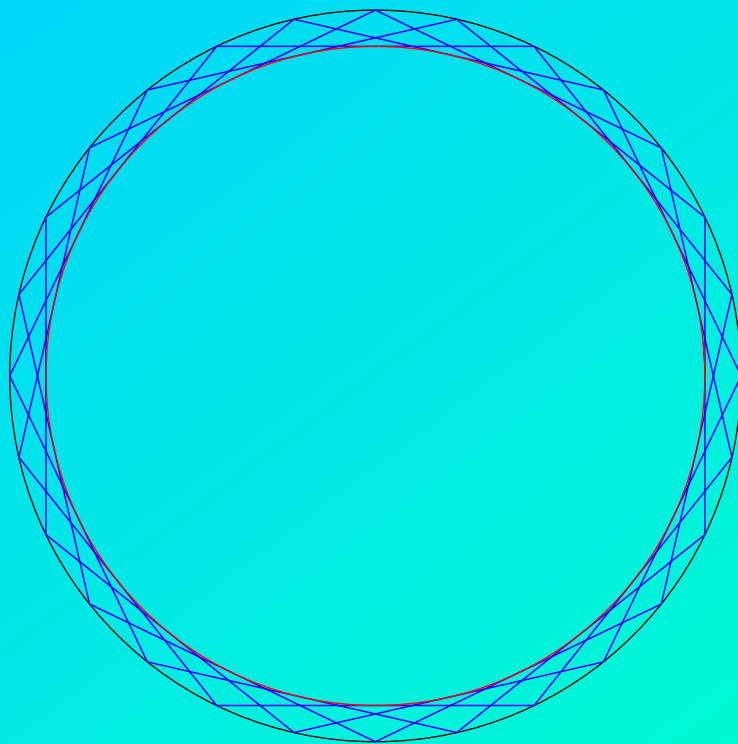


# Klasszikus biliárdok



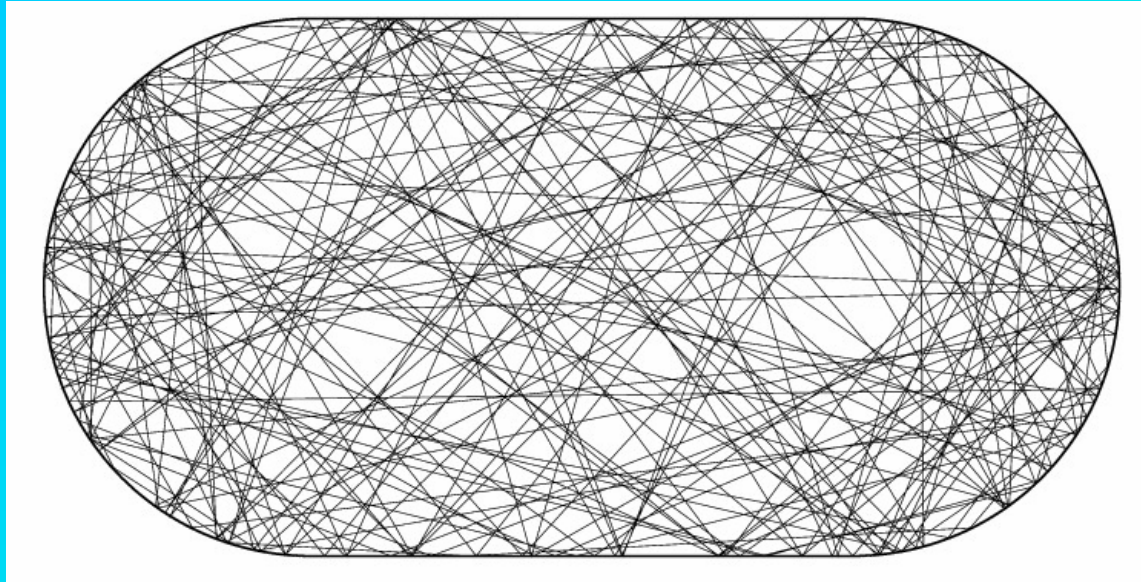
$N = 3$  pattogás a falon

$N = 7$  pattogás a falon





# Stadion biliárd



## Kaotikus biliárd



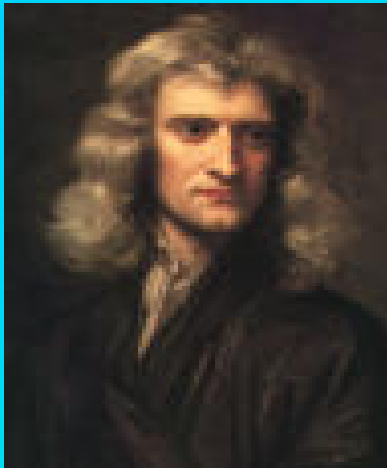
**Hendrik Antoon Lorentz**  
(1853-1928)

**Makroszkopikus világ**

**Mikroszkopikus világ**  
atomi méret

Klasszikus fizika

Kvantumfizika



**Sir Isaac Newton**  
(1643-1727)

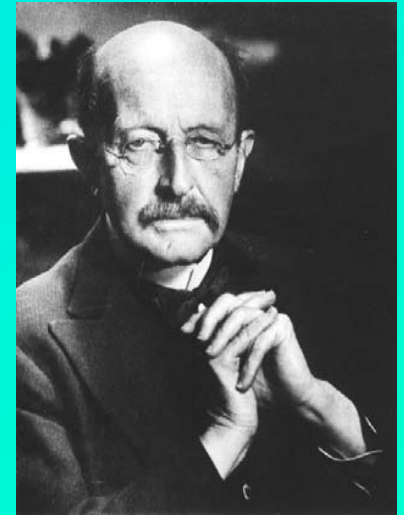


**Mezoszkopikus**

**Nanométeres** méretek

Kvantumfizika

**Nanofizika**




**Max Planck**  
(1858-1947)

# Mekkora 1nm ?

$$1\mu\text{m} = 1\text{mm} / 1000$$

$$1\text{nm} = 1\mu\text{m} / 1000$$

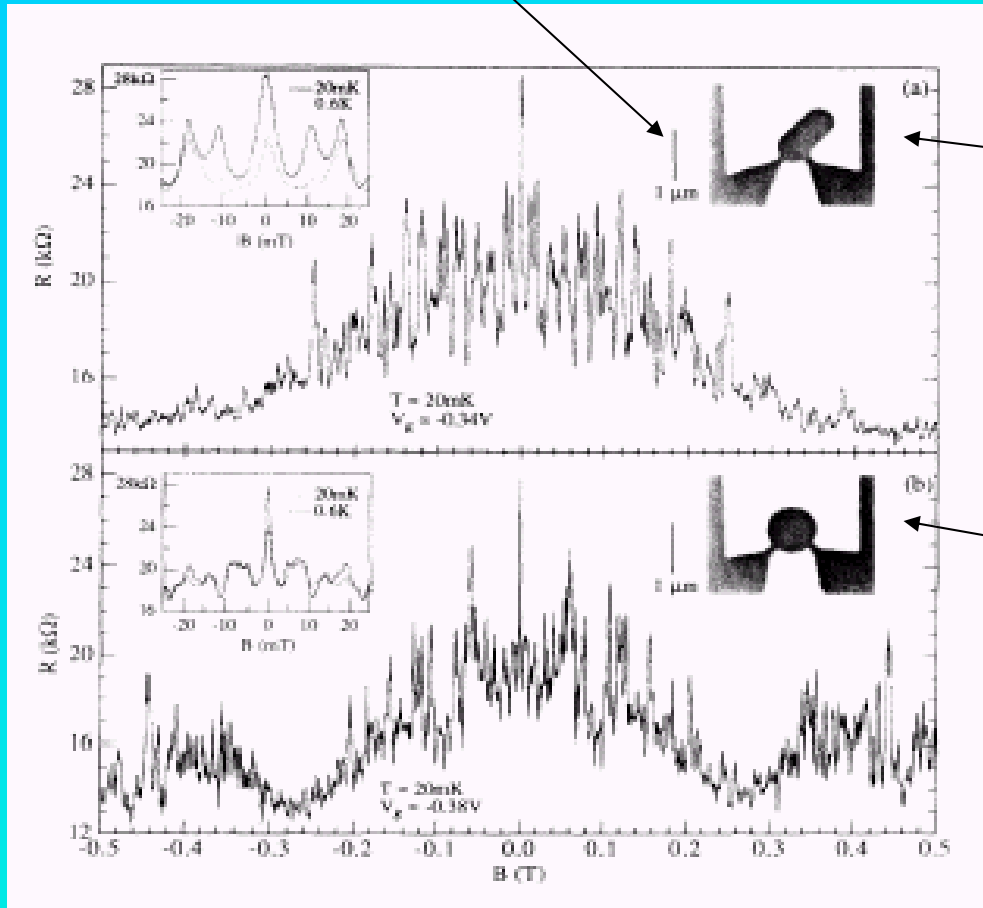
**1nm = 1 mm 1 milliomod része**

Ha a Nap – Föld = **1 m**  futballpálya = **1 nm**

# Kvantumbiliárdok Kísérleti megvalósítás

1992

1  $\mu\text{m}$



Stadion alakú

Kör alakú

A hőmérséklet  
mK alatt van

mágneses tér

Ellenállás

# Kvantumbiliárdok

A biliárd mérete: néhány száz nanométer

100 biliárd egy tű hegyén

elektron sebessége

kb. 2700 Km/sec

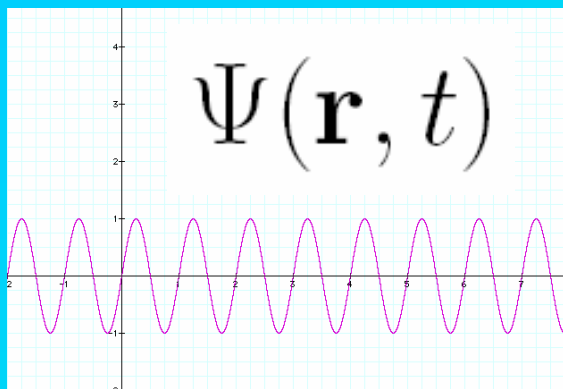
szabadúthossz < a biliárd méreténél

- nagy tisztaság
- alacsony hőmérséklet



# Kvantumfizika

de Broglie-hullám:



$$\lambda = \frac{h}{mv}$$

Planck-állandó

elektron sebessége

$$|\Psi|^2$$

Az elektron megtalálási valószínűsége

Schrödinger-egyenlet



lemez mozgása

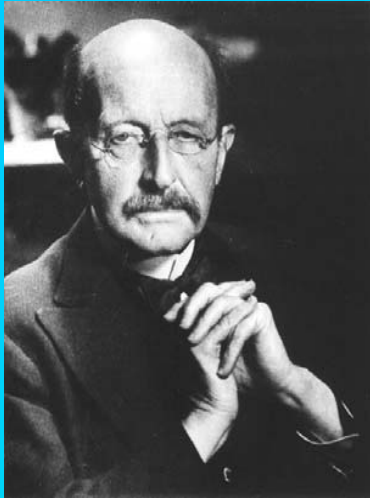


$\Psi(\mathbf{r}, t)$  hullámfüggvény



$u(\mathbf{r}, t)$  a lemez kitérése

# Kvantumfizika



**Max Planck**  
(1858-1947)



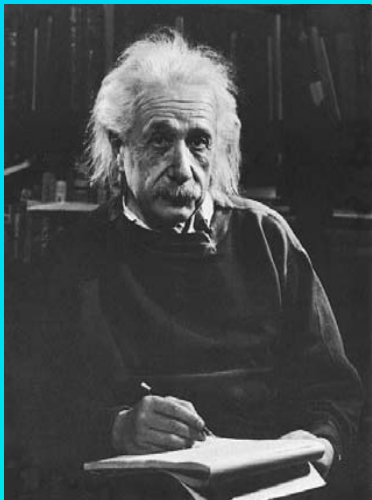
**Niels Bohr**  
(1885-1962)



**David Hilbert**  
(1862-1943)



**Louis de Broglie**  
(1892-1981)



**Albert Einstein**  
(1879-1955)



**Erwin Schrödinger**  
(1887-1961)



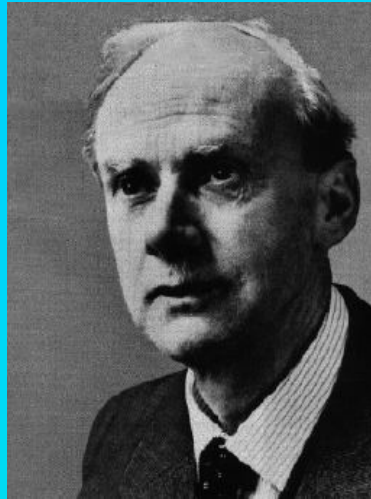
**Werner Heisenberg**  
(1901-1976)



**Wigner Jenő**  
(1902-1995)



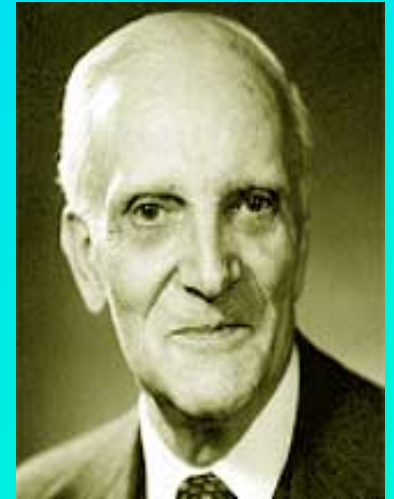
**Wolfgang Pauli**  
(1900-1958)



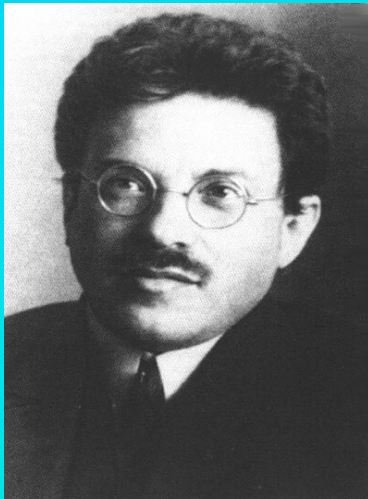
**Paul Dirac**  
(1902-1984)



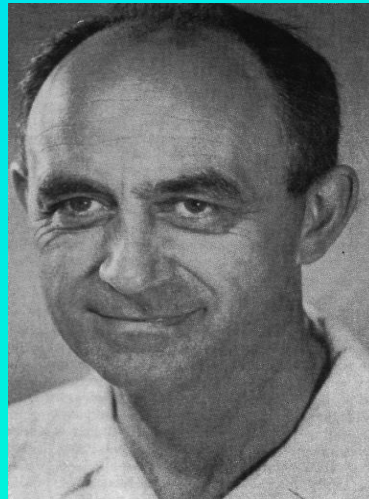
**Neumann János**  
(1903-1957)



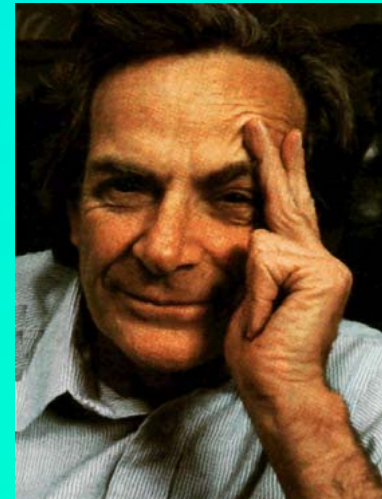
**Leon Brillouin**  
(1889-1969)



**Paul Ehrenfest**  
(1880-1933)



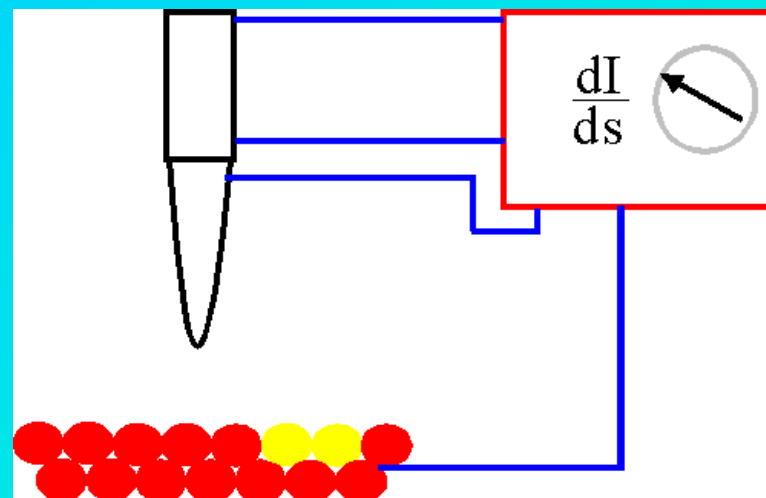
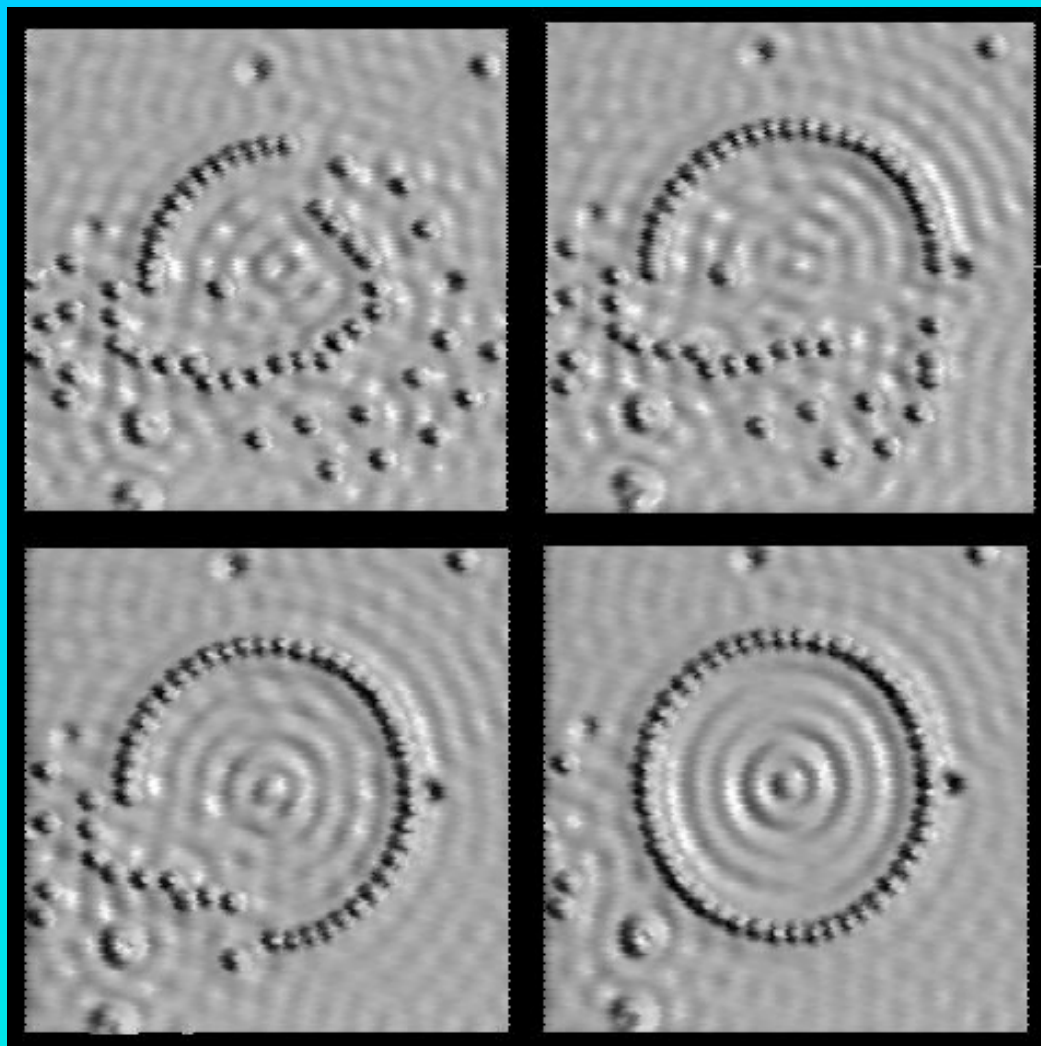
**Emerico Fermi**  
(1901-1954)



**Richard Phillips Feynman**  
(1918-1988)

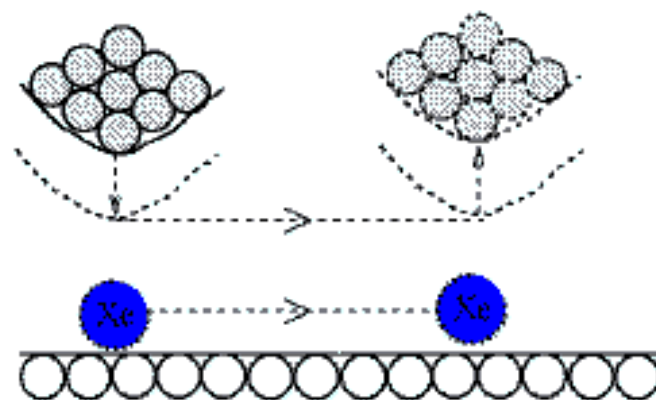


# Pasztázó alagútmikroszkóp



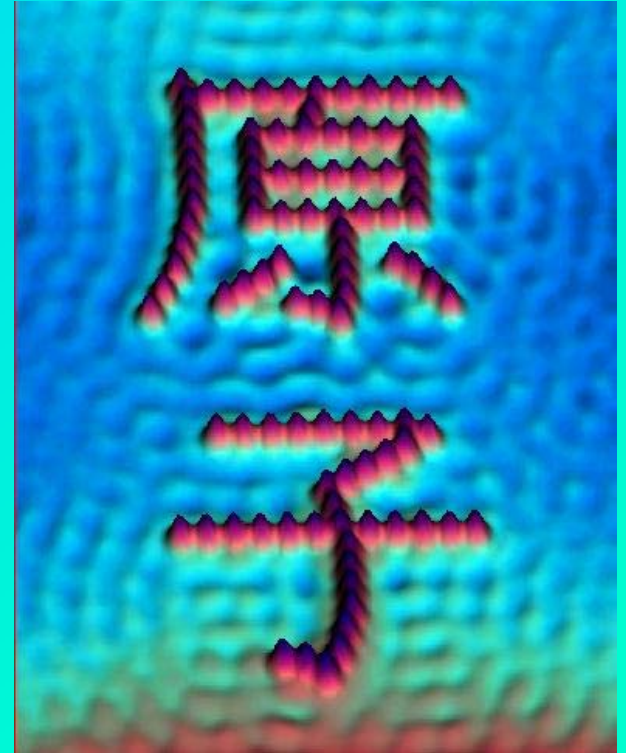
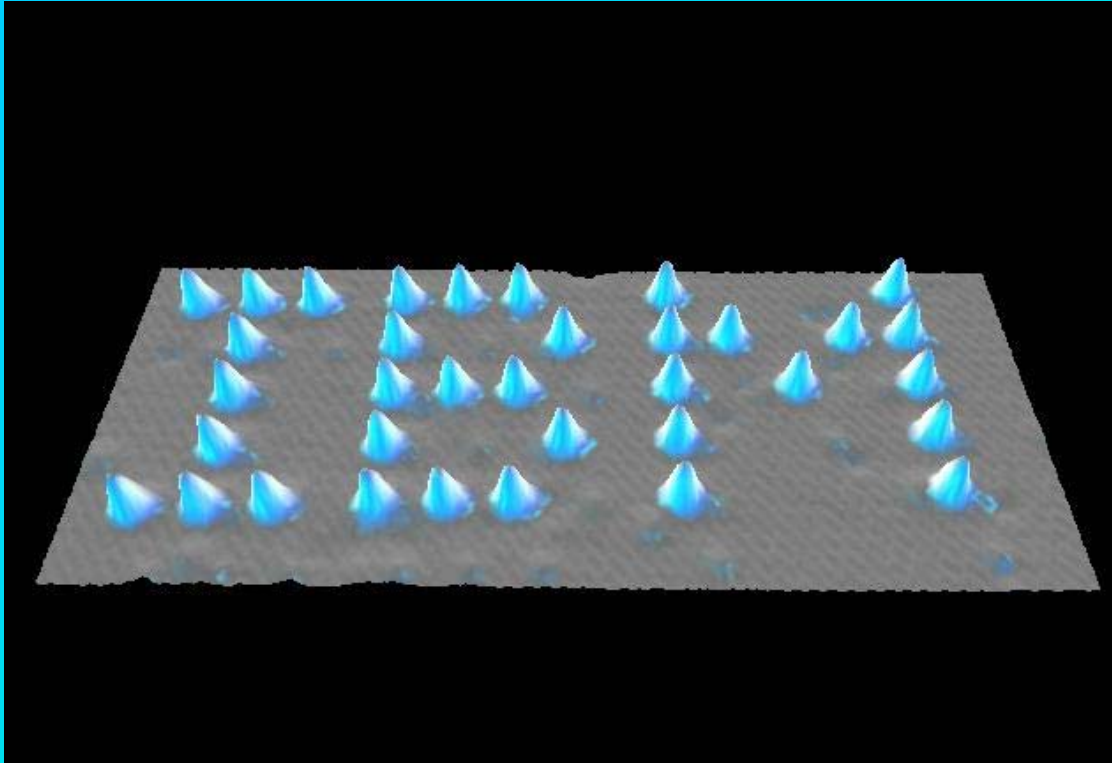
## Positioning Atoms with an STM

D.M. Eigler & E.K. Schweizer Nature 344 524 (1990)



The STM tip is brought down near the atom, until the attraction is enough to hold it as the atom is dragged across the surface to a new position.

# Atomok elhelyezése egy felületen

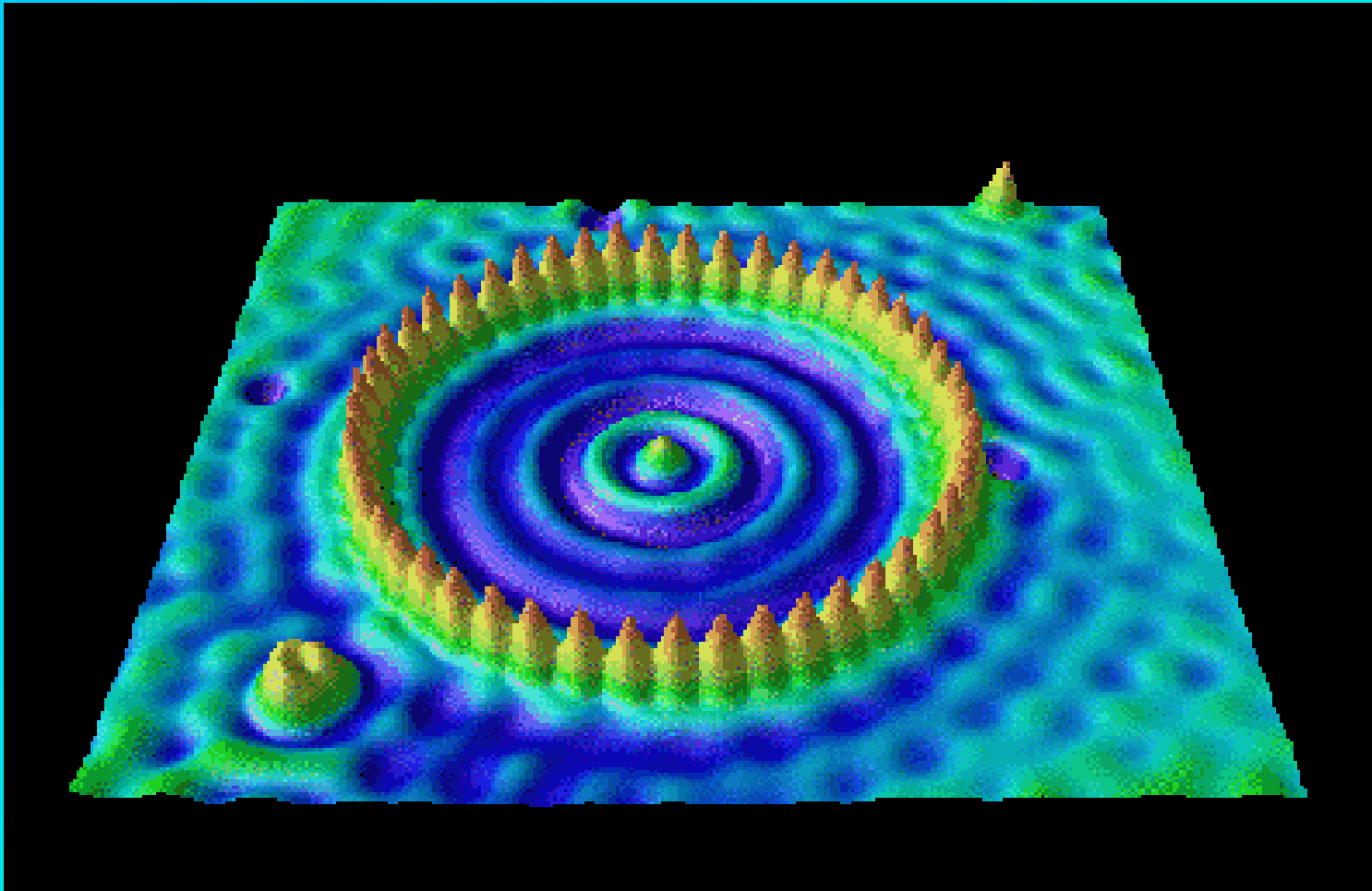


35 Xenon atom Nickel felületen,  
*He* hőmérsékleten, IBM Zürich Research Laboratory 1990



# Kvantum karám

Cu lapon elhelyezett 48 Fe atom egy  $R=71,8 \text{ \AA}$  sugarú kör mentén  
*elektron-állóhullámok*

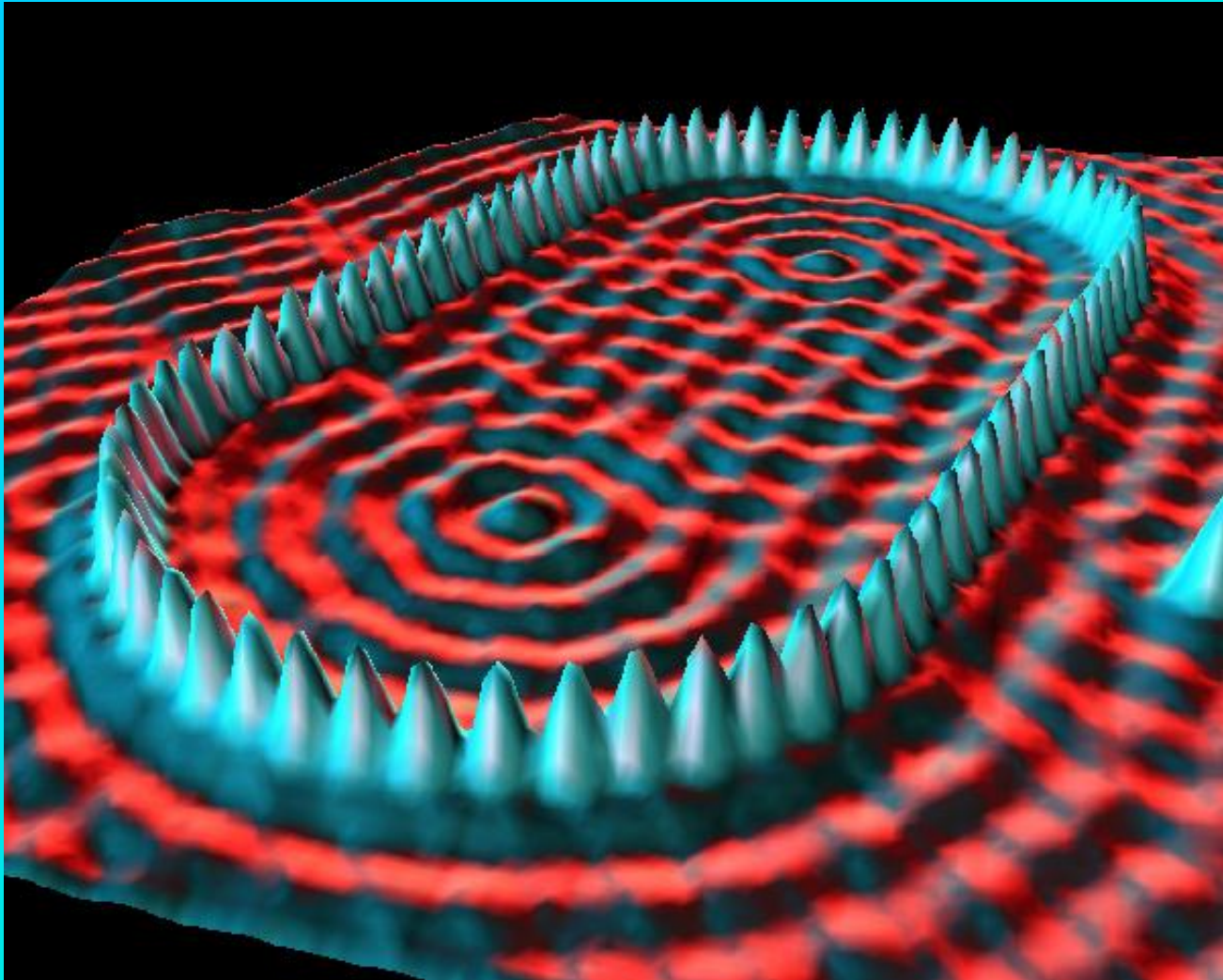


$$|\Psi|^2$$

mérése

# Kvantum stadion

1995



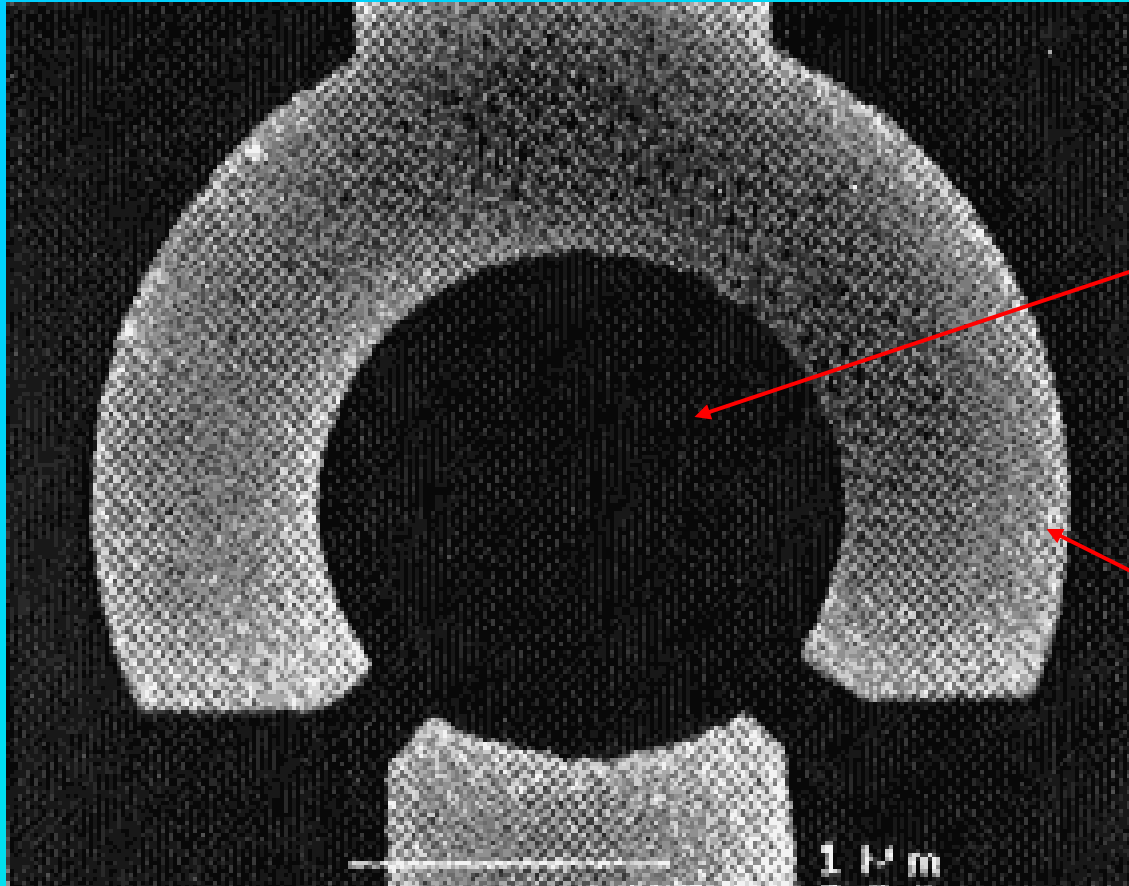
M.F. Crommie, C.P. Lutz, D.M. Eigler, E.J. Heller. Waves on a metal surface and quantum corrals.

*Surface Review and Letters* 2 (1), 127-137 (1995).

Cs. J.: KÖMAL 2004. április szám



# Mezozkopikus biliárd



elektronok 2 dimenzióban

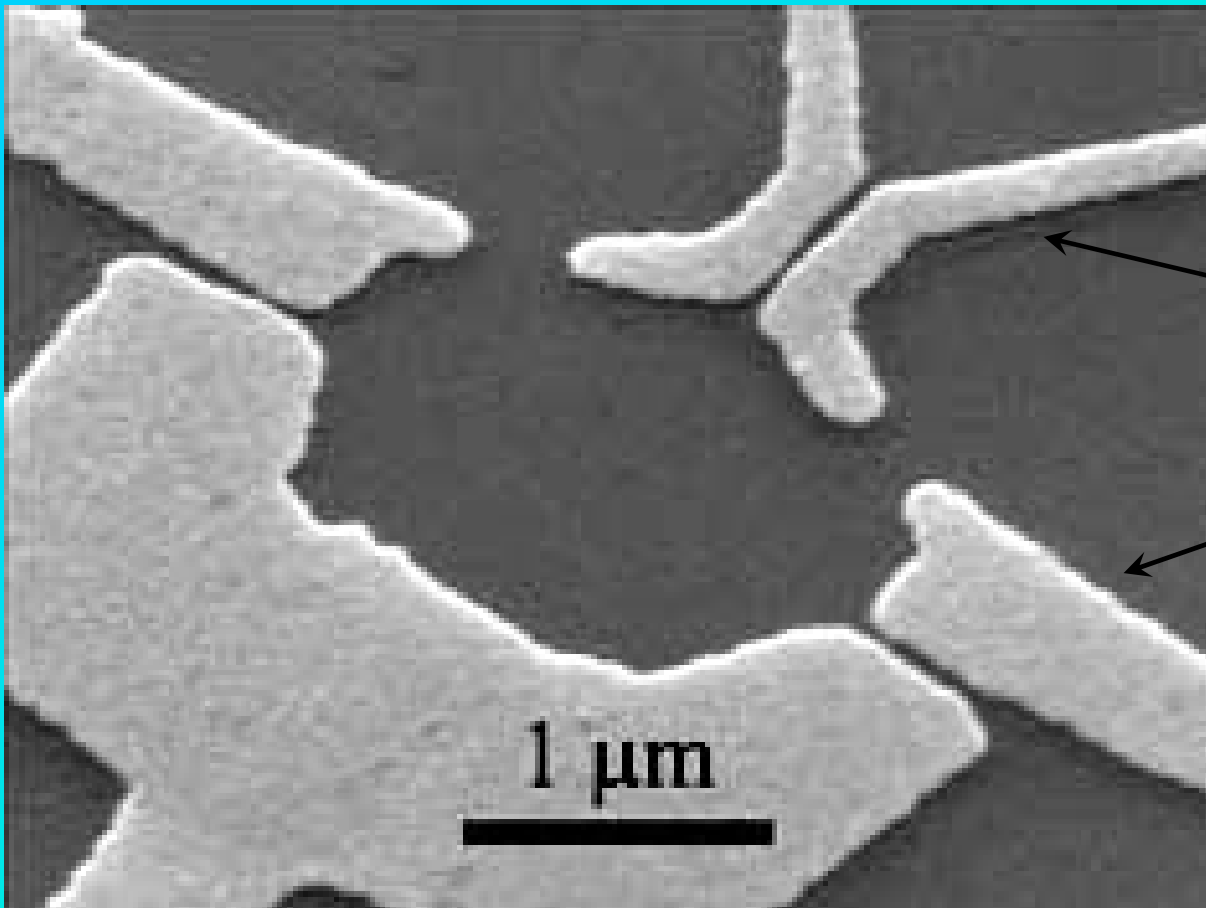
elektródák

Az elektron a fekete tartományban mozog,  
elkerülve az elektródákat

1994

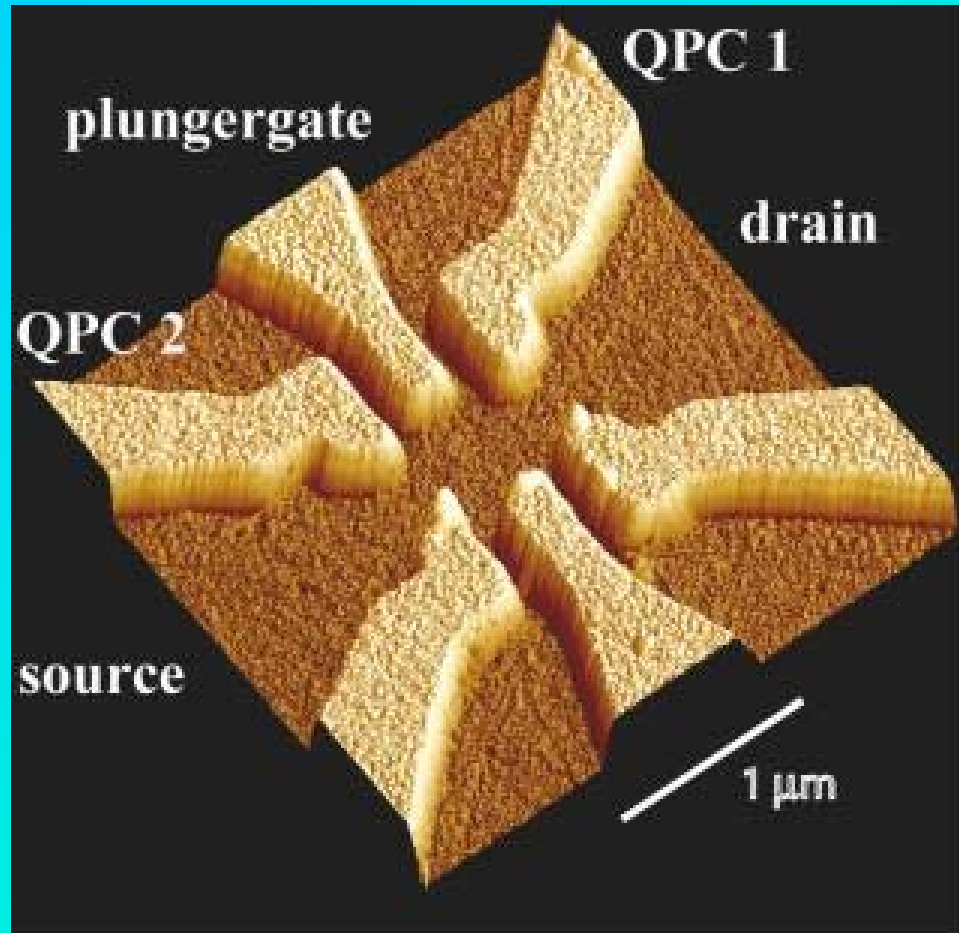
# Kvantum pöttyök

Elektron mozgása kétdimenzióban  
GaAs félvezető-rétegszerkezetben



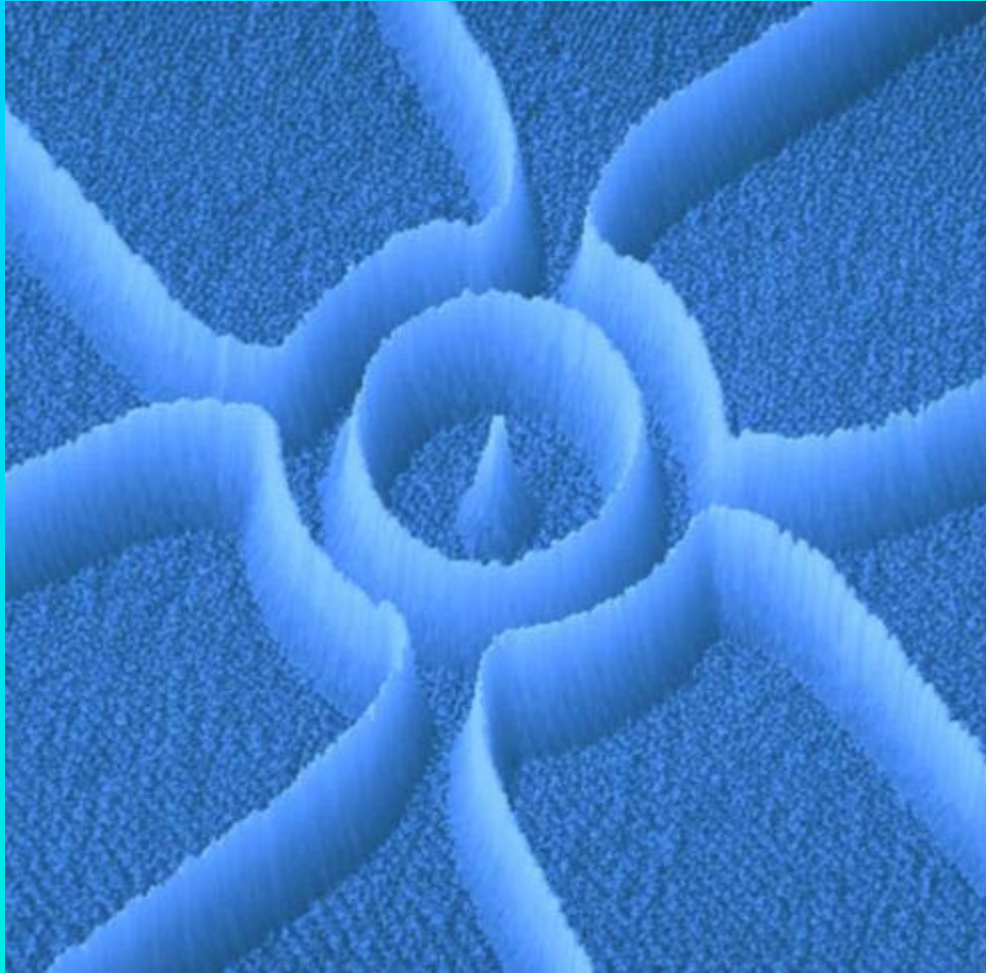
Negatíván  
töltött elektrodák

# Kvantum pöttyök



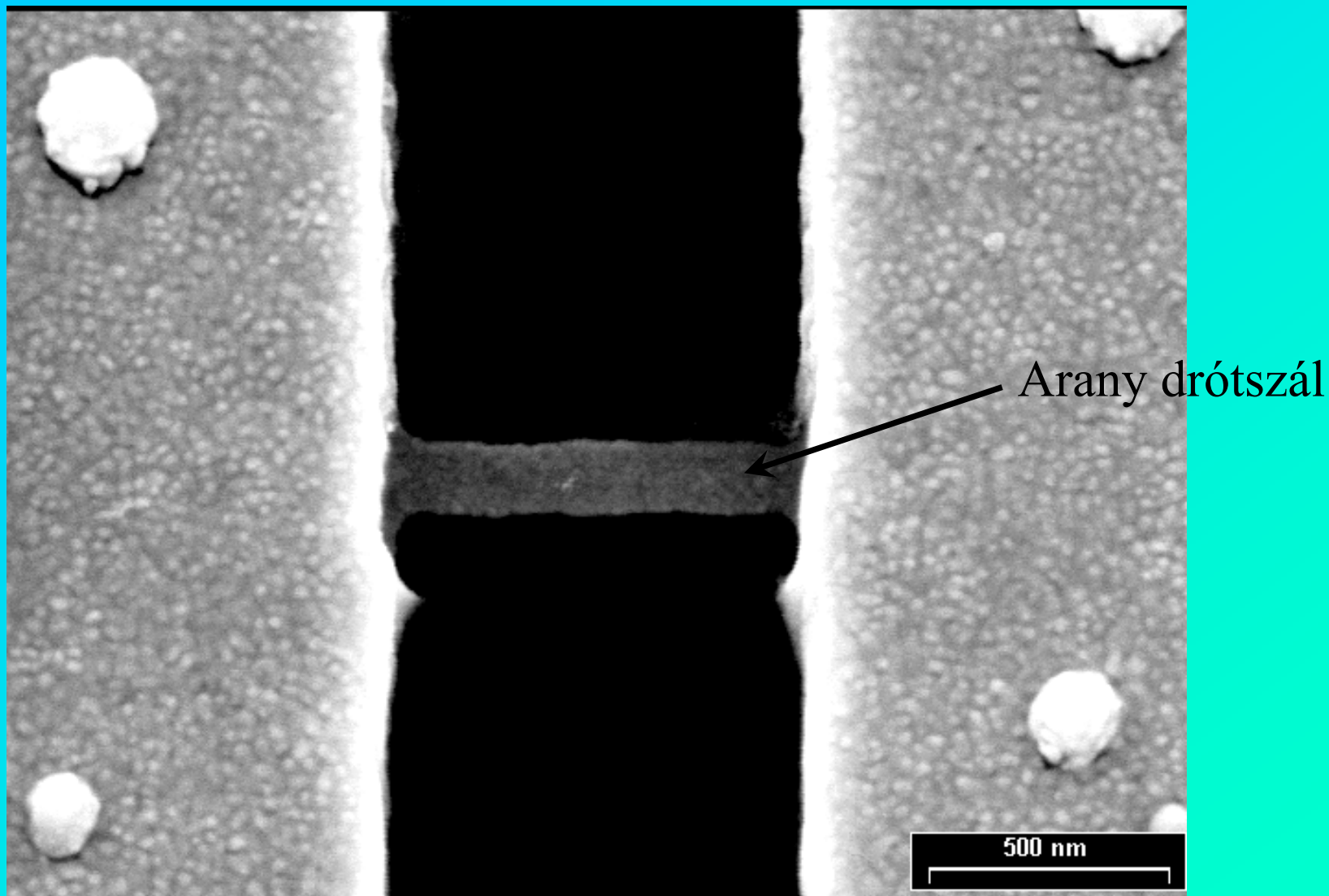


# Kvantum gyűrűk

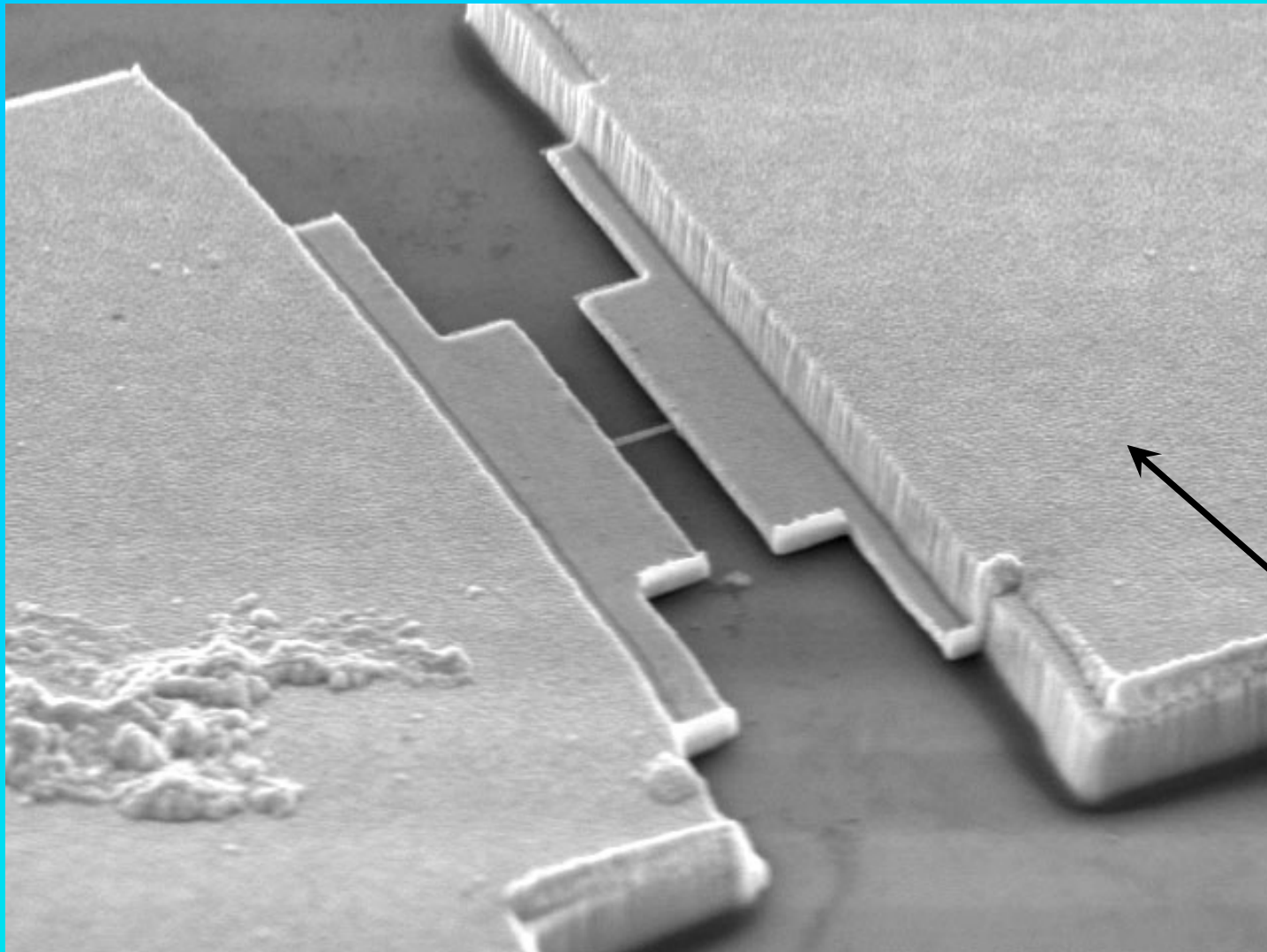


NCCR Nanoscale Science  
Institute of Physics, University of Basel

# Nanodrótok



áram kb. 0,1 mA



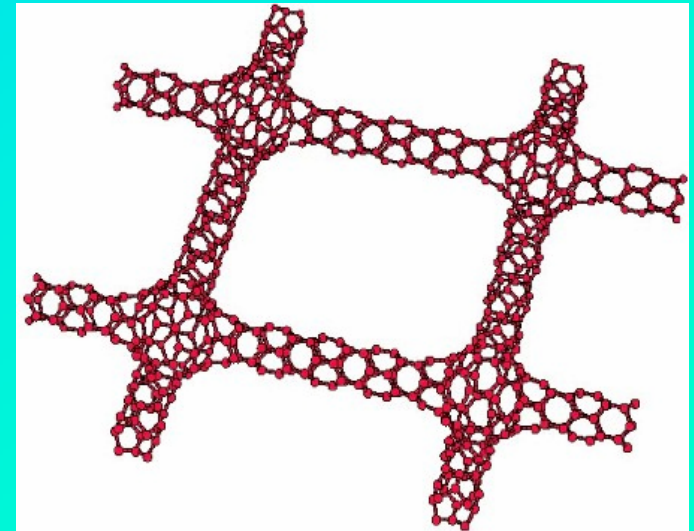
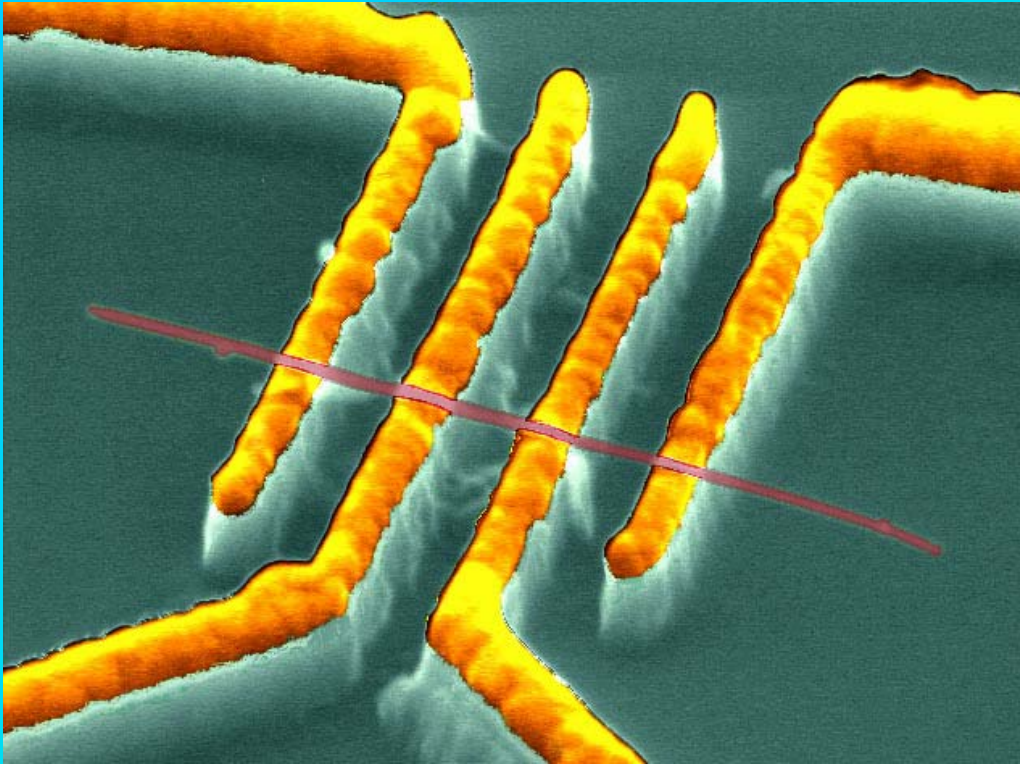
Hőmérséklet  
270 mK

Cu tömb

100 nm széles, 1 mm hosszú Au drót



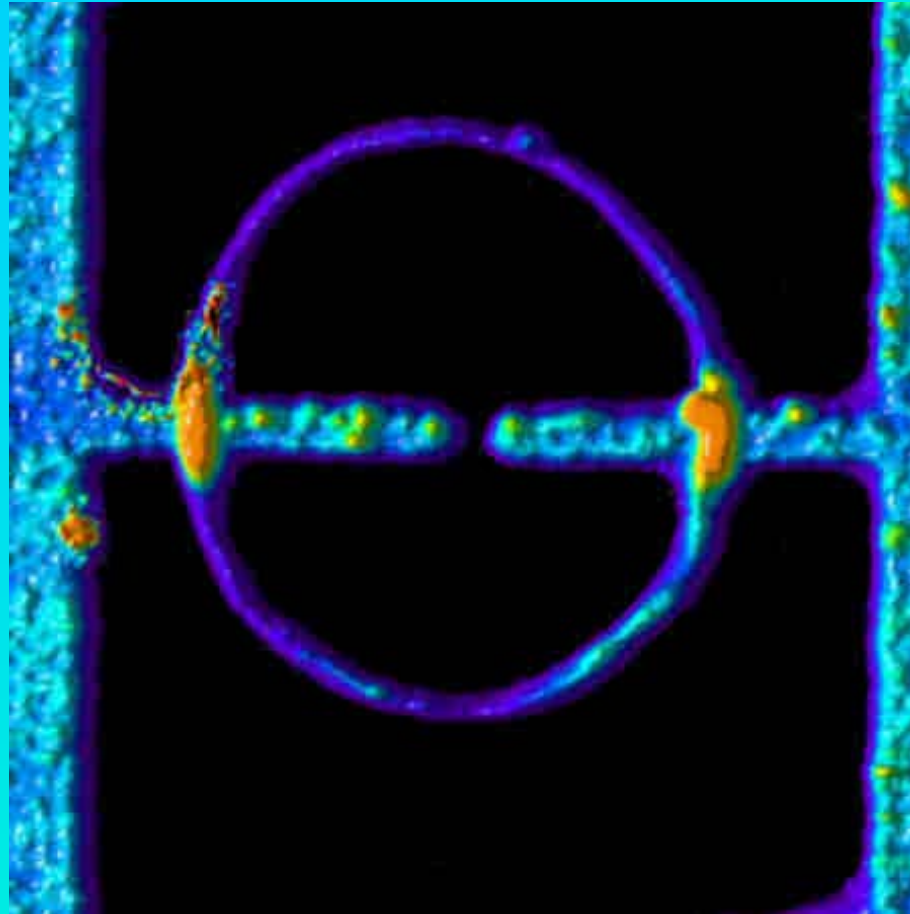
# Szén nanocsövek



**Kürti Jenő:** Szén nanocsövek: mik azok és mire jók?  
(Az atomoktól a csillagokig)

# Szén nanocsőből készült karika

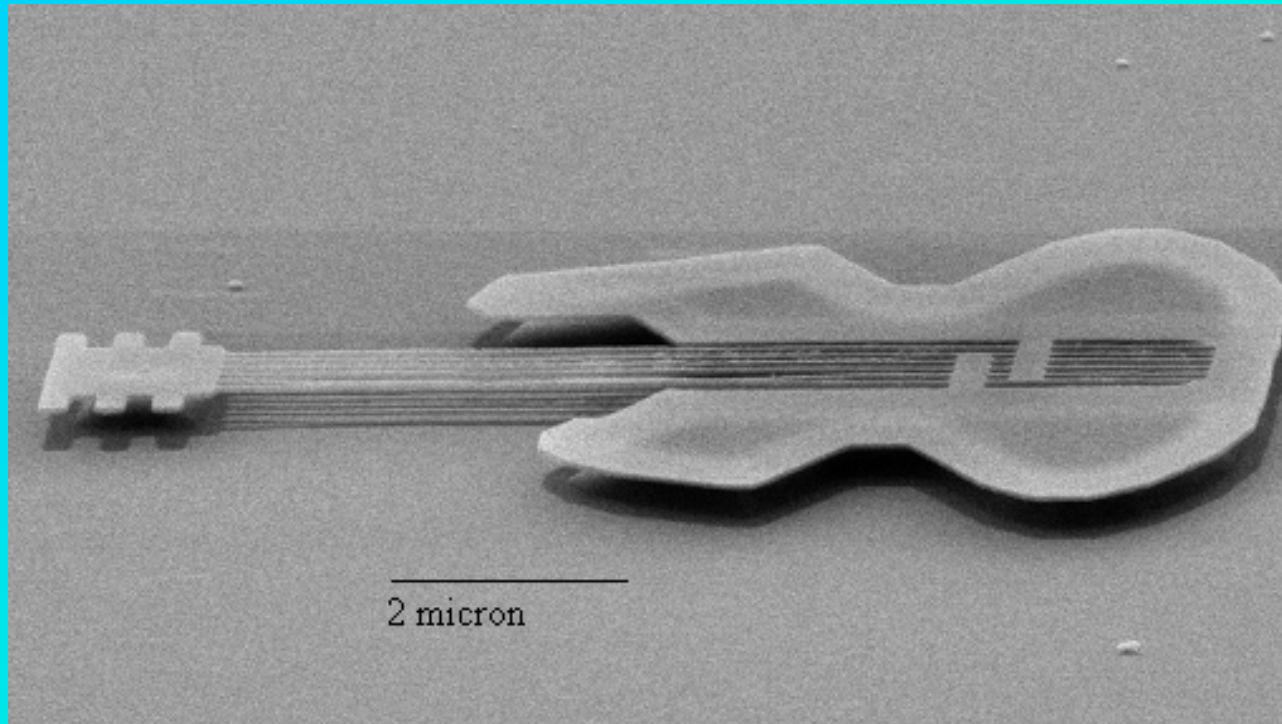
$R = 700 \text{ nm}$



Electrical Transport in Rings of Single-Wall Nanotubes: One-Dimensional Localization"  
Phys. Rev. Lett. 84 (19) 4441. 8 May 2000

# Nano gitár

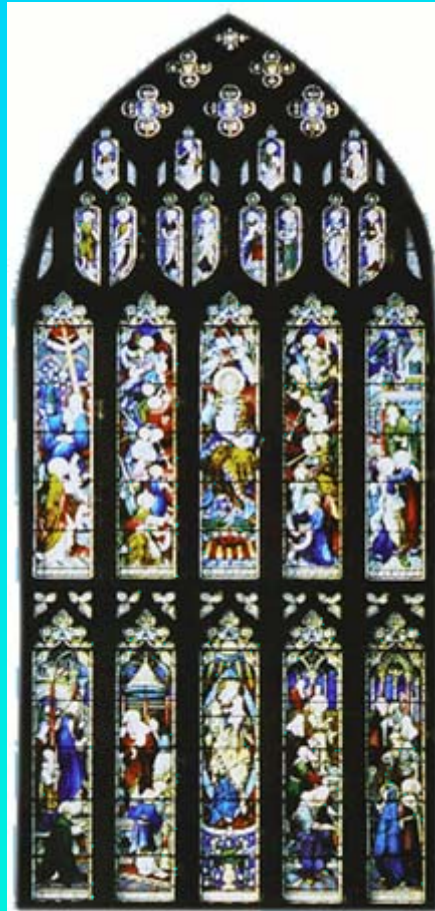
A világ legkisebb gitárja, hossza  $10\ \mu\text{m} = 1/100\ \text{mm}$ ,  
a hajszál vastagságának 20-ad része!





# Templomok színes ablakai

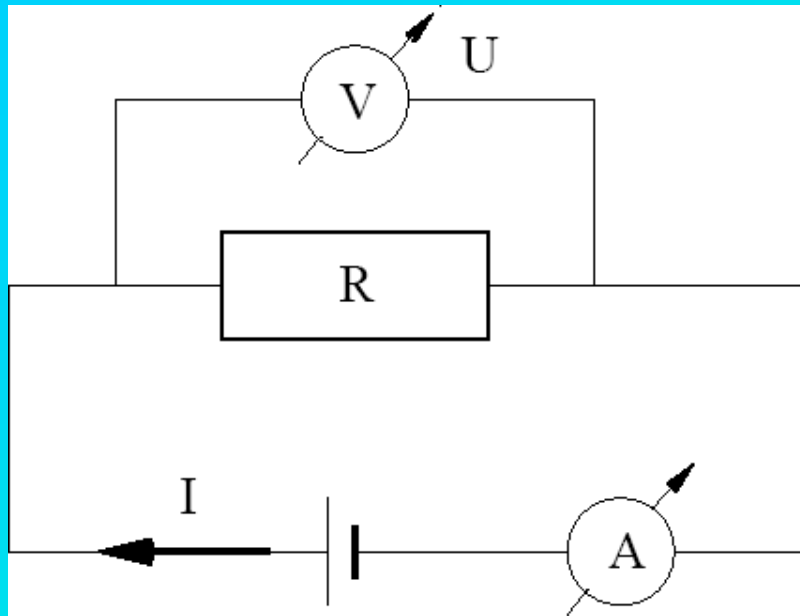
Nanométer méretű fém szemcséket kevertek az üvegbe



Már a 10. században alkalmazták

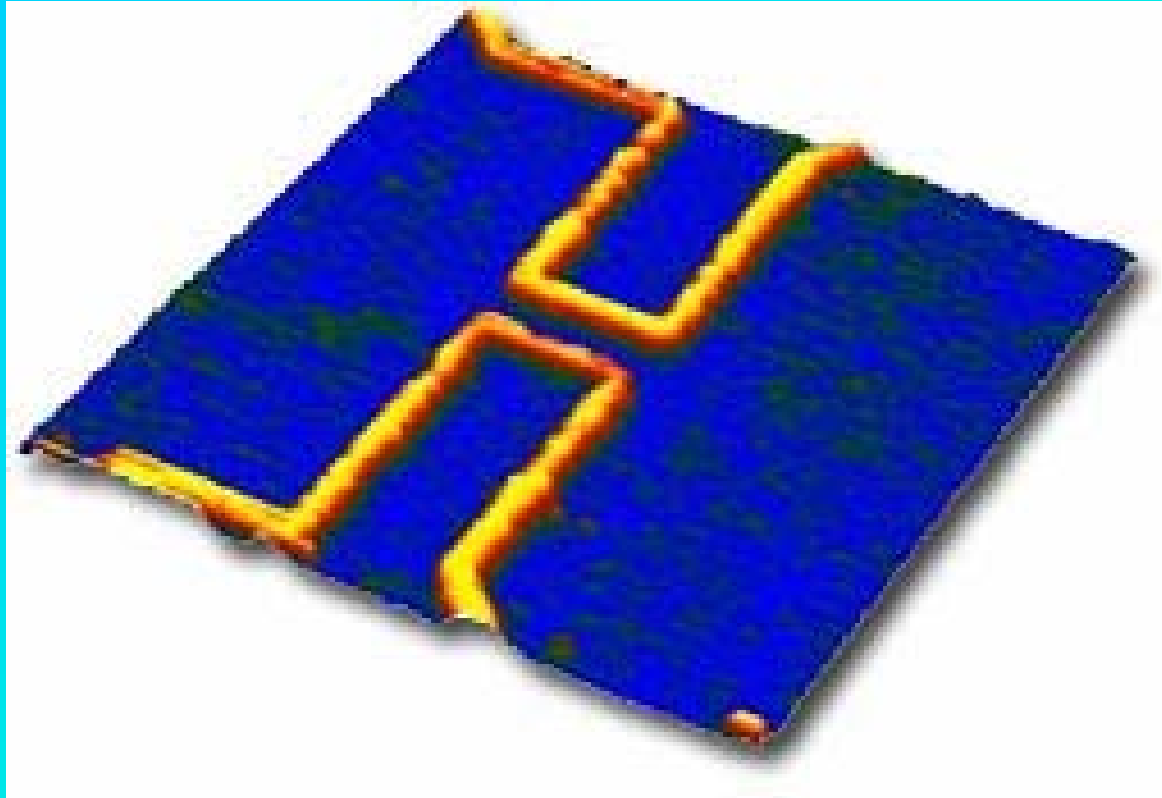
# Ohm-törvénye

## Az ellenállás



$$R = \frac{U}{I}$$

# Nem igaz az Ohm-törvény a nanofizikában!



# Ellenállás kvantum

$$R = \frac{1}{N} \frac{h}{2e^2}$$

Planck-állandó

Egész szám

Elektron töltése

$$\frac{h}{2e^2} = ?$$

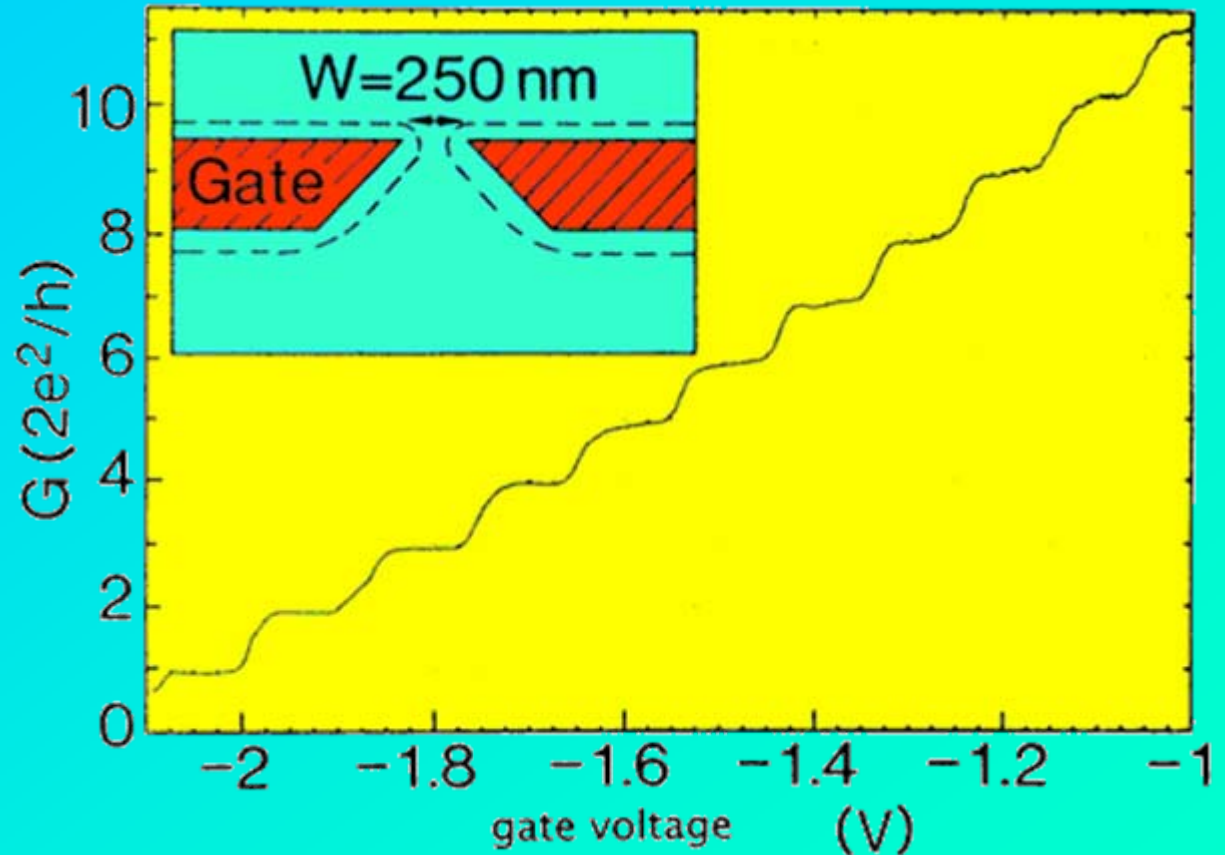
$$\frac{h}{2e^2} = 12906 \Omega = 12,906 k\Omega$$

# Az első mérés

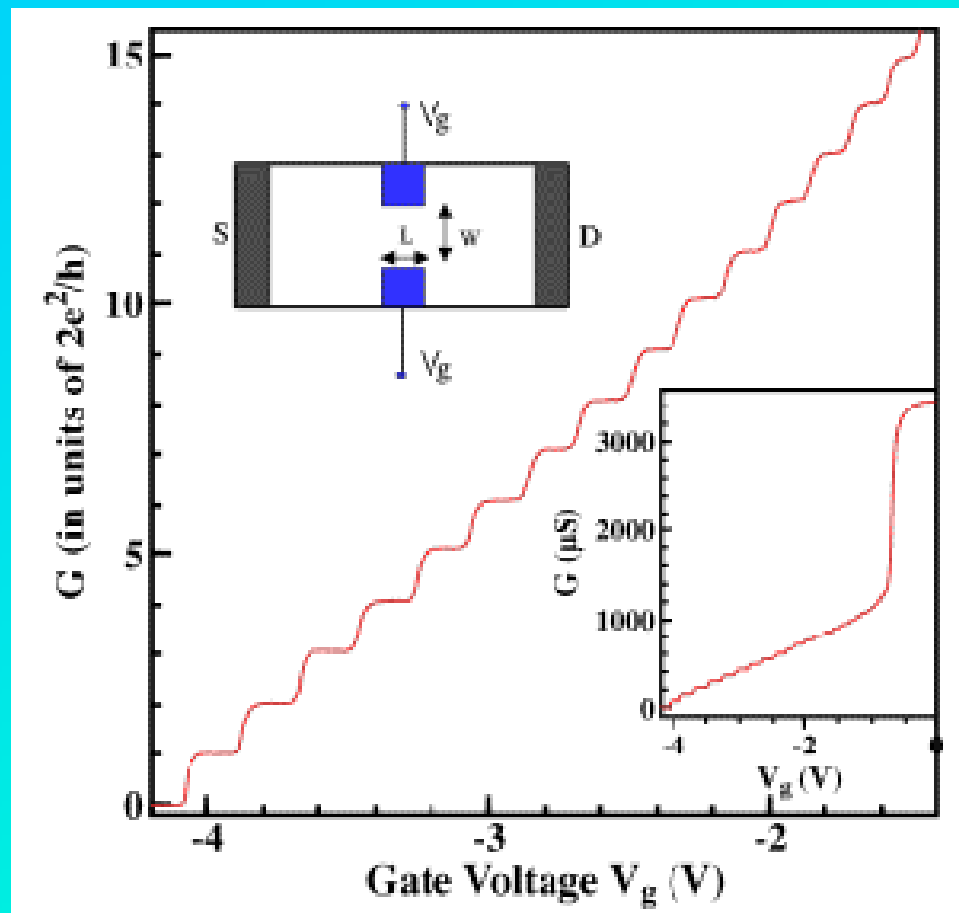
1988

Vezetőképesség,  
az ellenállás reciproka

$$G = \frac{1}{R} = N \frac{2e^2}{h}$$



B. J. van Wees et al., *Phys. Rev. Lett.* **60**, 848 (1988)





# Adattárolás

„There’s Plenty of Room at the Bottom.”

Richard Feynman, 1959

100 atom  $\longrightarrow$  1 bit információ

0,1 mm élű kocka  $\longrightarrow$  Világ összes írott anyaga

KÁROLYHÁZY FRIGYES

**IGAZ  
VARÁZSLAT**



GONDOLAT ZSEBKÖNYVEK

„Napjainkban bontakozik ki a hatékony logikát és harmonikus szépségélményt kínáló természettudományos világkép.”

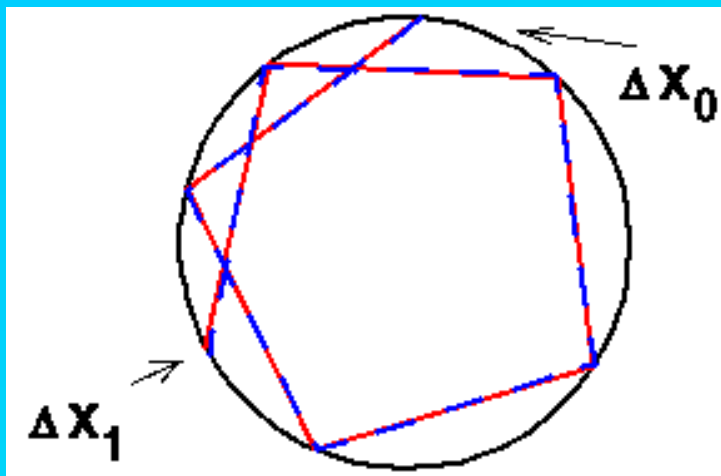
**Marx György: Életrevaló atomok**

„Hogy átsző mindent az Egész!  
Egyik a másikba hat s tenyész!”

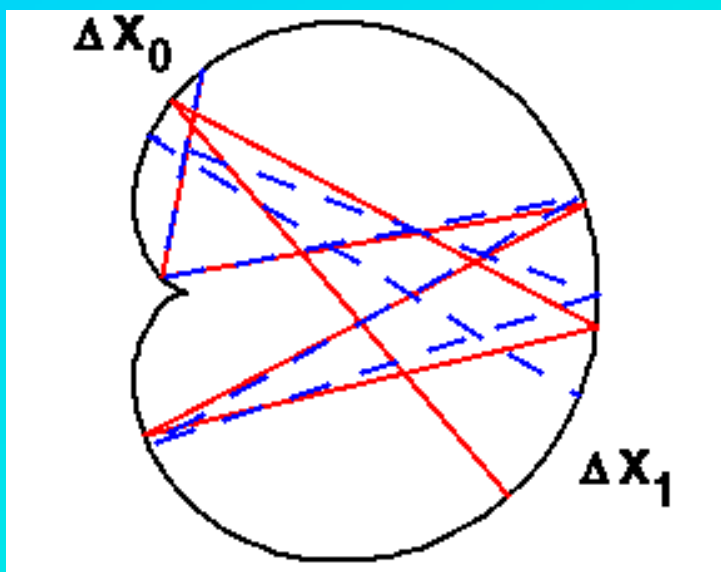
**Goethe: Faust** (Jékely Zoltán fordítása)

„A kvantummechanikáról szólni száz oldalon olyan feladat, mint egy induló vonat ablakából szerelmet vallani.”

**Károlyházi Frigyes: Igaz varázslat**



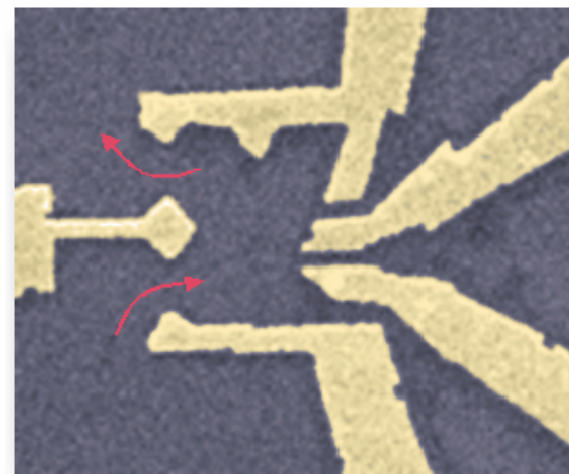
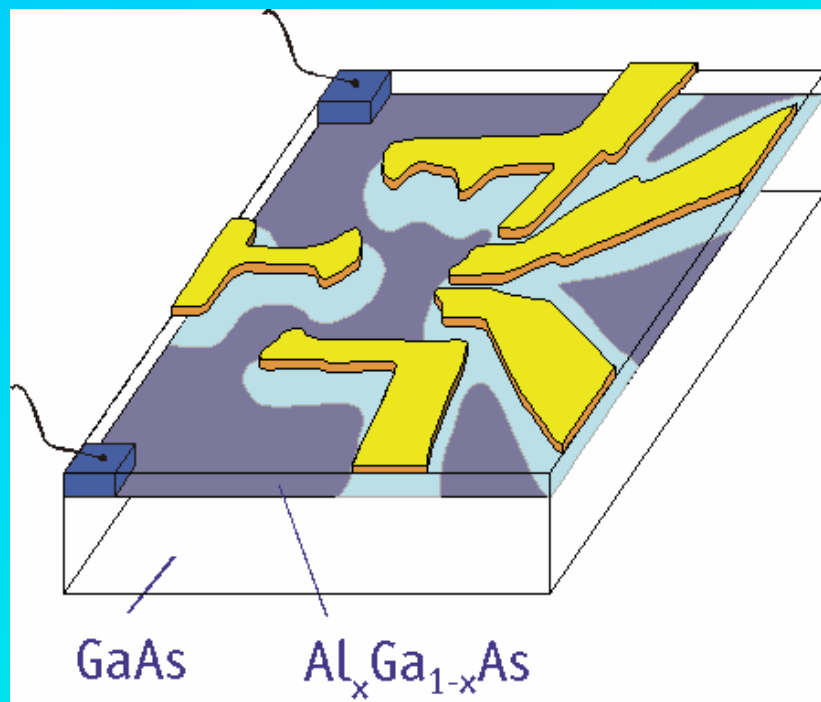
**Nem** érzékeny  
a kezdőfeltételre



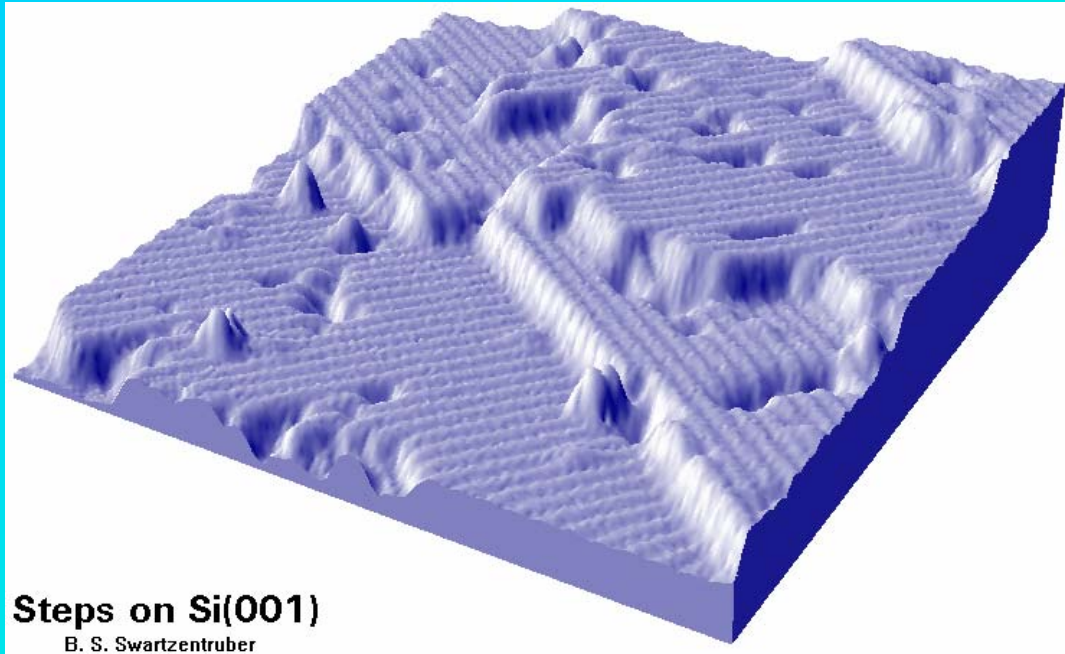
**Érzékenység**  
a kezdőfeltételre



**Kaotikus biliárd**



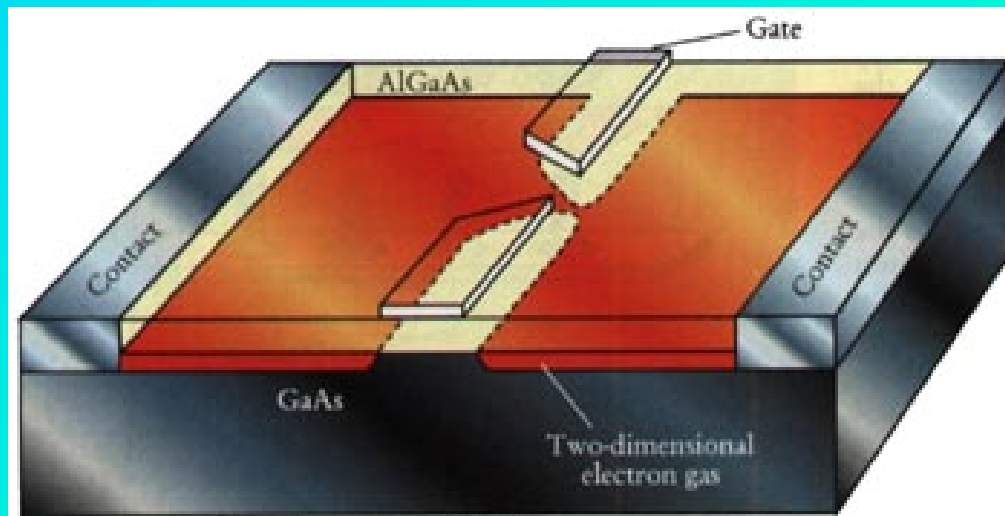
1 μm



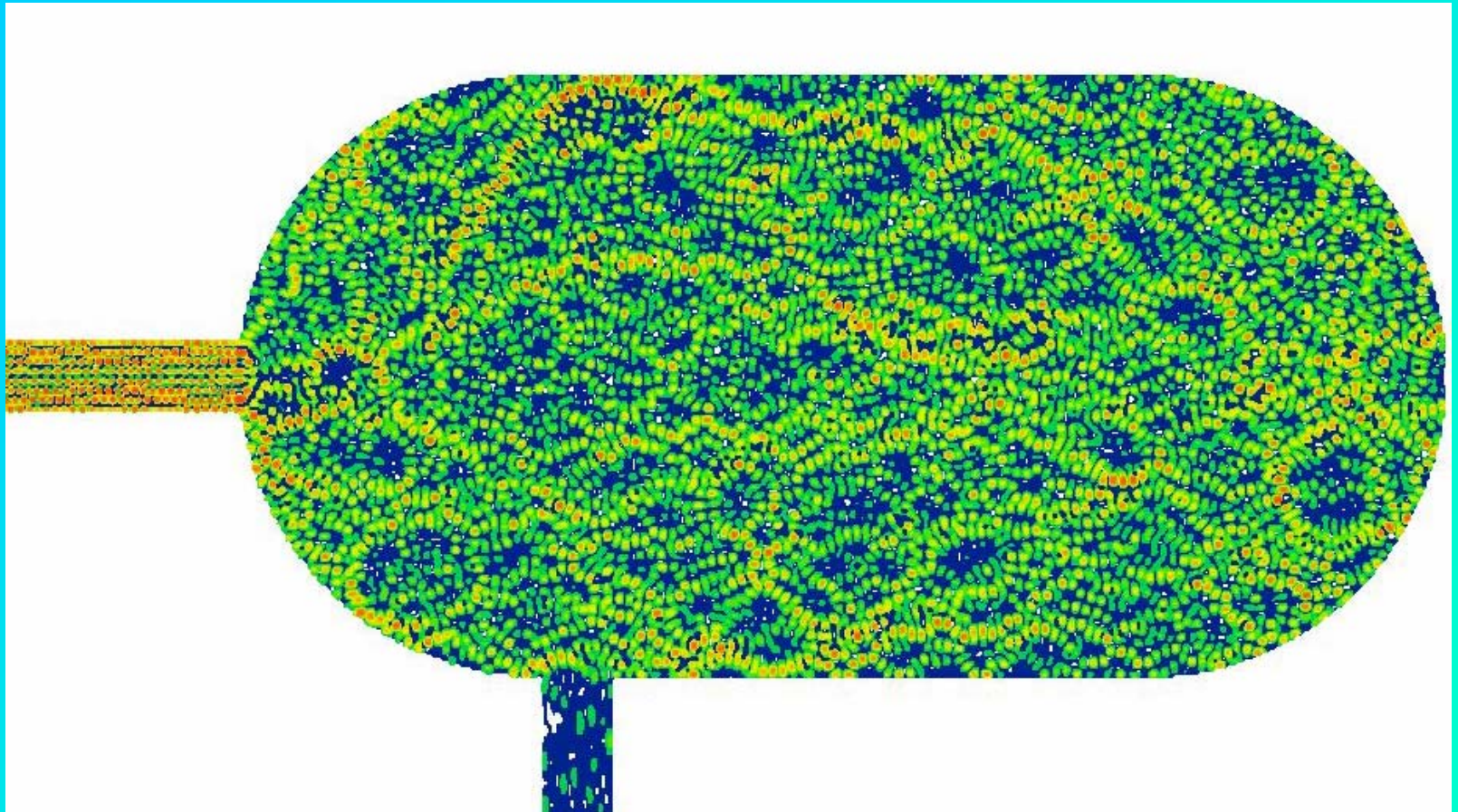
**Steps on Si(001)**

B. S. Swartzentruber

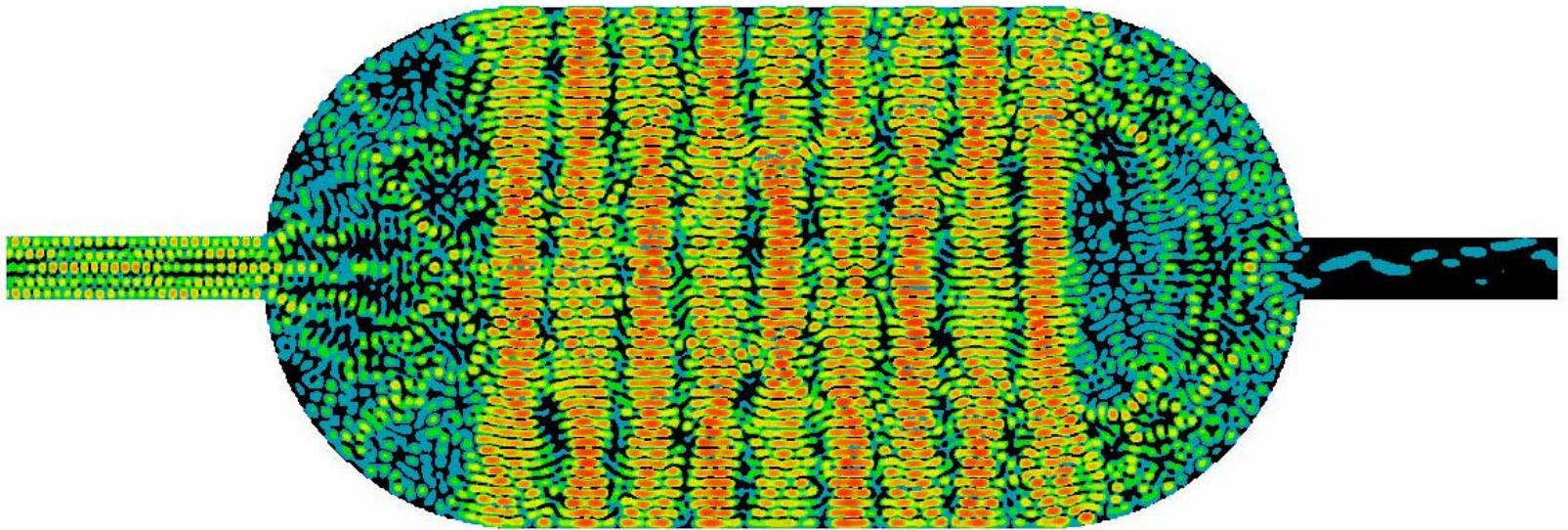




# Hullámfüggvény stadionban

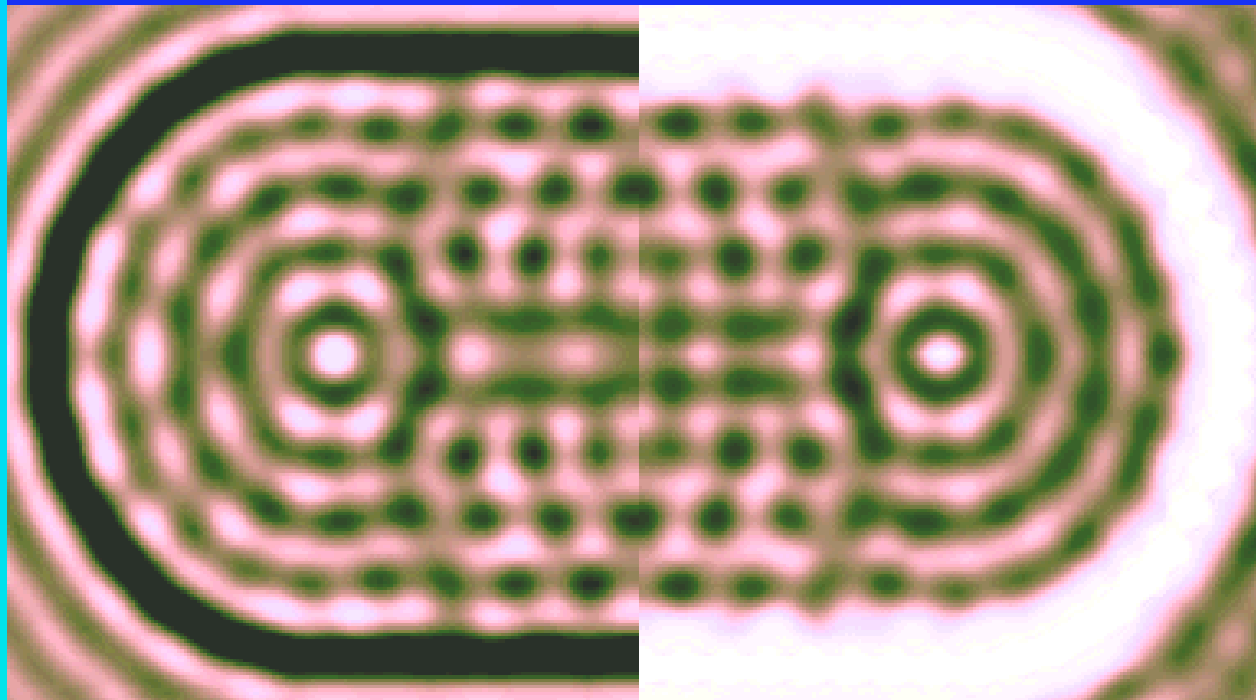


# Pattogó módus



*Theory*

*Experiment*



*STM Image of 76 Atom Corral*