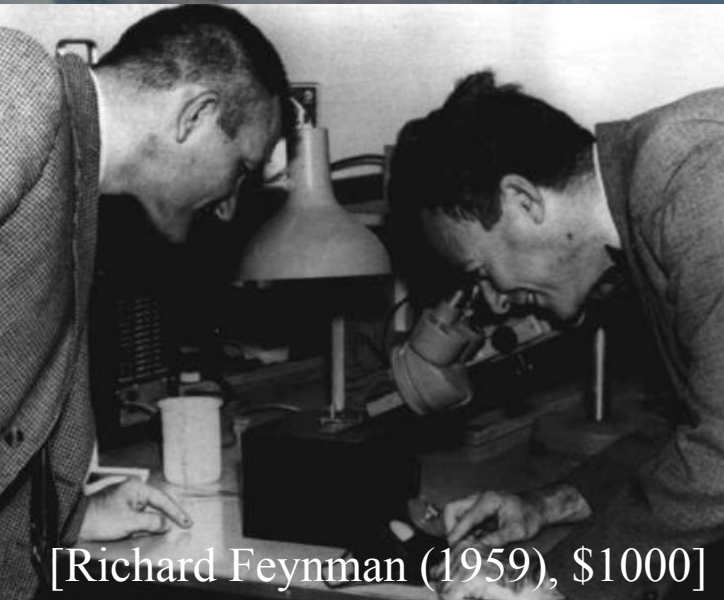


# Molekuláris motorok: hogyan működnek és mi a biológiai szerepük?

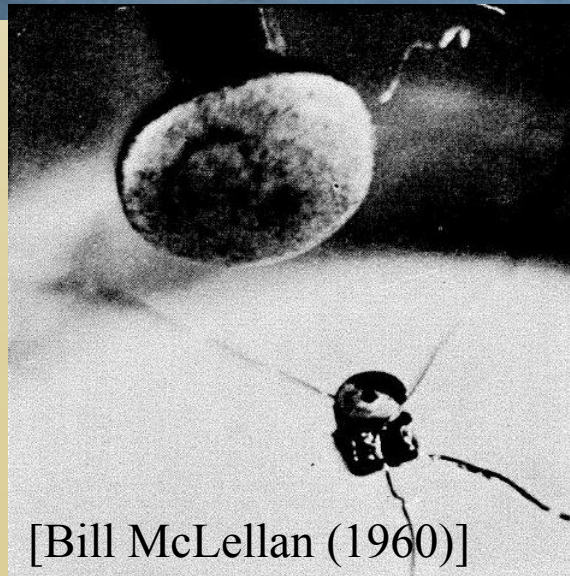


Derényi Imre

*ELTE TTK, Biológiai Fizika Tsz.*



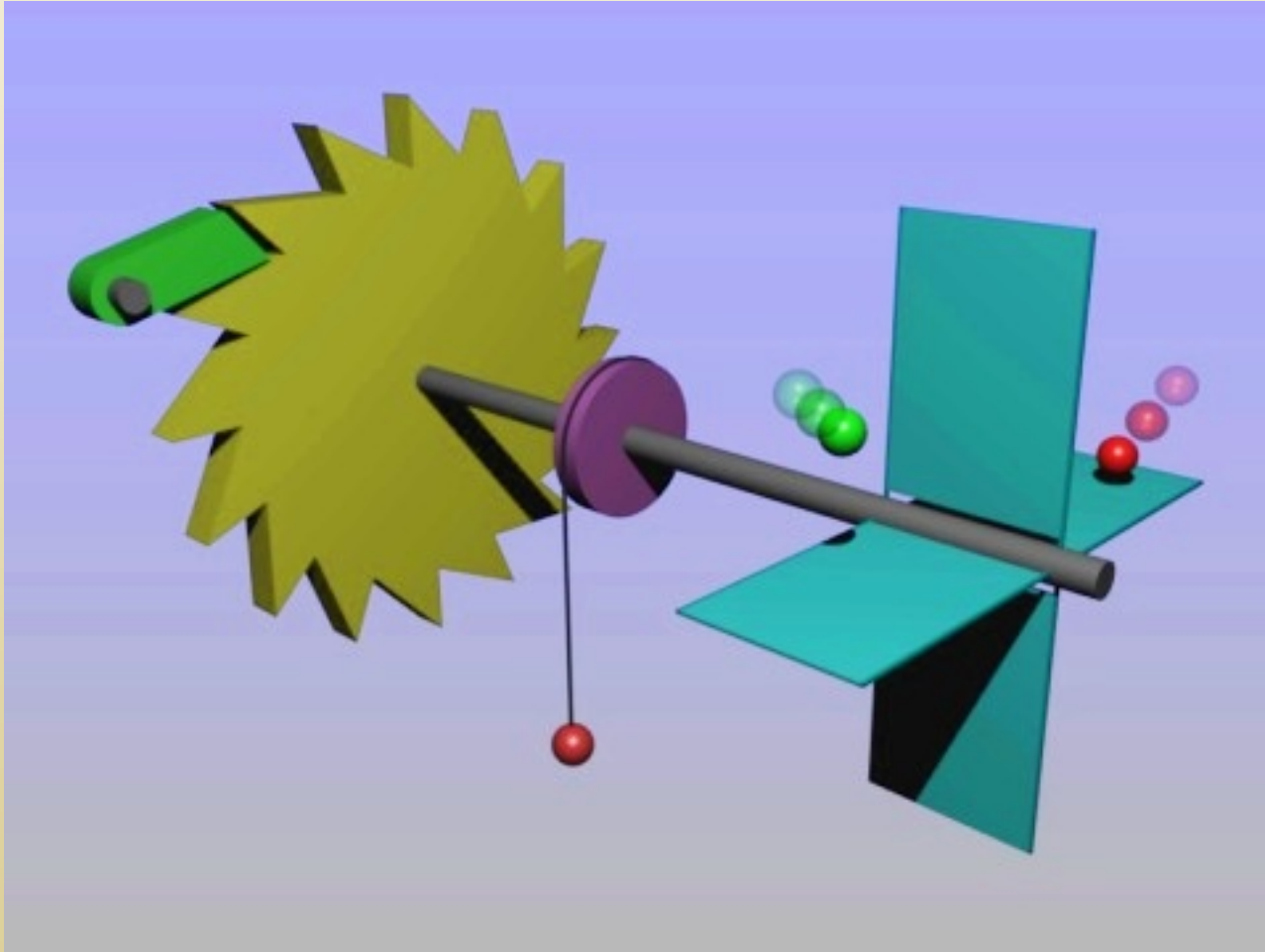
[Richard Feynman (1959), \$1000]



[Bill McLellan (1960)]

*Atomcsill - 2010*

# Feynman racsni (kilincskerék)

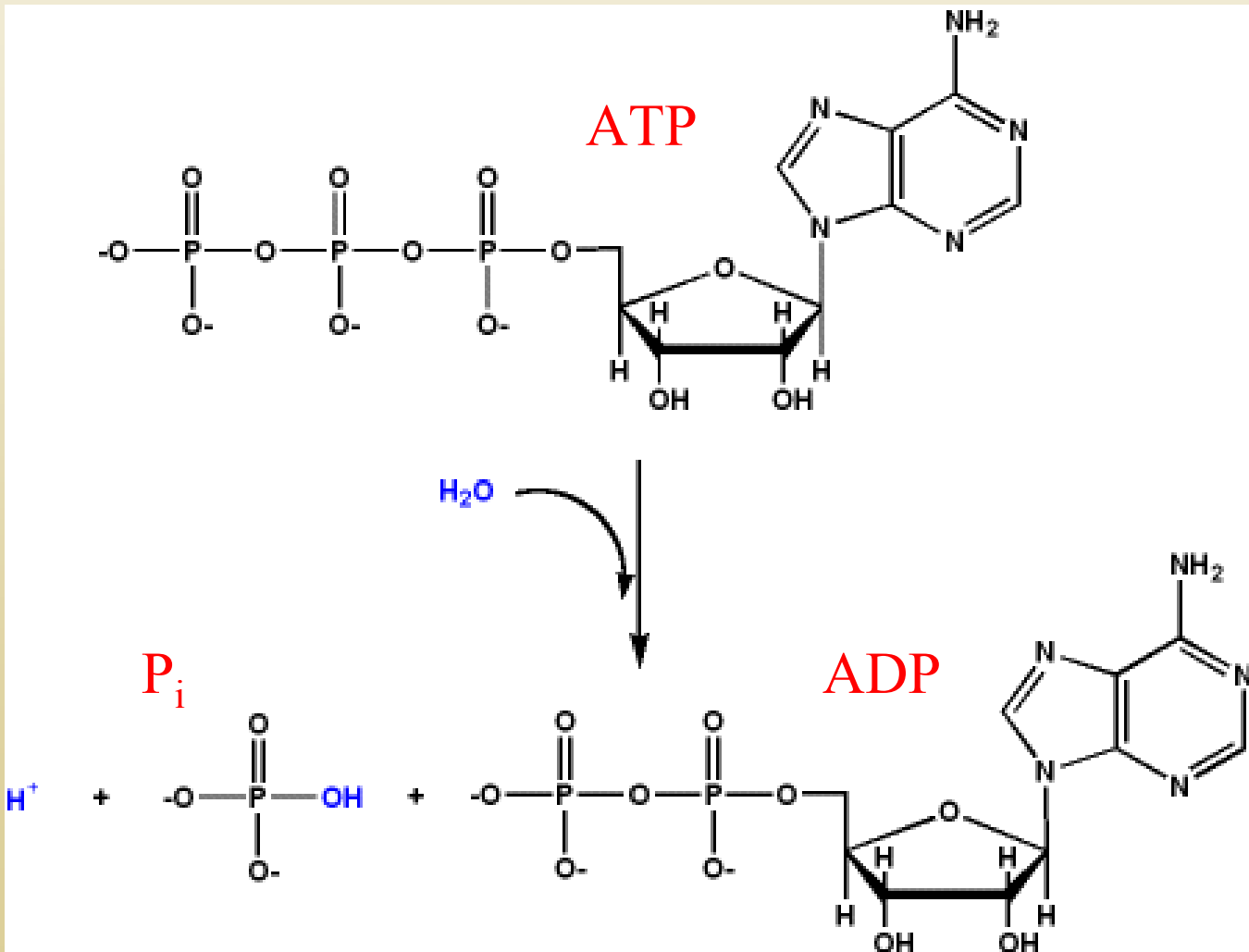


# Szabadenergia (üzemanyag)

A szabadenergia biológiailag legalapvetőbb formái:

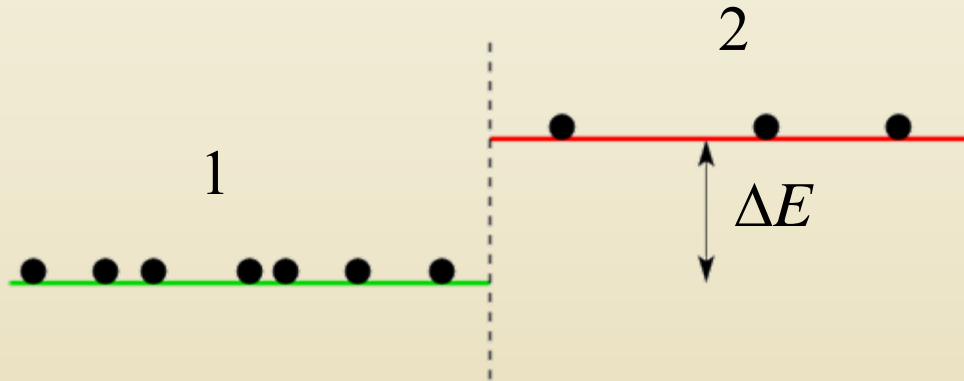
- kémiai kötési energia
- koncentrációkülönbség
- elektrosztatikus potenciálkülönbség

# kémiai kötési energia (ATP hidrolízis)



~100 pN nm

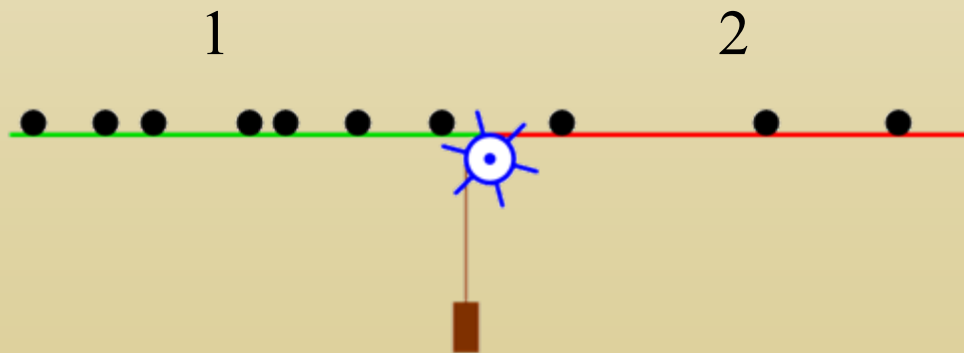
# koncentrációkülönbség



Boltzmann eloszlás:

$$c_2 = c_1 e^{-\frac{\Delta E}{k_B T}}$$

$$\Delta E = k_B T (\ln c_1 - \ln c_2)$$



Maximális munkavégzés  
részecskénként:

$$W = k_B T (\ln c_1 - \ln c_2)$$

# Fizika a molekuláris méretskálán

## Makroszkópikus világ:

- (a) gyengén csillapított mozgás (nagy Reynolds szám);
- (b) hőmérsékleti fluktuációk elhanyagolhatók.

## Következmények:

- (a) az időskálákat a sebességek és gyorsulások határozzák meg;
- (b) a zaj kiküszöbölhető.

## Mikroszkópikus világ:

- (a) túlcsillapított mozgás, tehetetlenség elhanyagolható (alacsony  $Re$ );
- (b) a hőmérséklet vadul rázza a molekulákat.

## Következmények:

- (a) az időskálákat termális folyamatok határozzák meg (diffúzió, aktiváció);
- (b) a hőmérsékleti zaj kihasználható.

# Hőmérsékleti fluktuációk

hőmérsékleti energia:

$$k_B T \approx 1.38 \times 10^{-23} \text{ J/K} \cdot 300 \text{ K} \approx 4 \times 10^{-21} \text{ J} = 4 \text{ pN nm}$$

ekvipartíció:  $\frac{1}{2} m \langle v^2 \rangle = \frac{1}{2} k_B T$

$$v \approx \sqrt{\frac{k_B T}{m}} \approx \sqrt{\frac{4 \times 10^{-21} \text{ J}}{18 \times 10^{-3} \text{ kg} / 6 \times 10^{23}}} = \sqrt{\frac{4}{3} 10^5 \frac{\text{m}}{\text{s}}} \approx 350 \frac{\text{m}}{\text{s}}$$

$$mgh = k_B T$$

$$h = \frac{k_B T}{mg} = \frac{4 \times 10^{-21} \text{ J}}{18 \times 10^{-3} \text{ kg} / 6 \times 10^{23} \cdot 10 \text{ m/s}^2} = \frac{4}{3} 10^4 \text{ m} \approx 13 \text{ km}$$

# Túlcsillapított mozgás

$$m\dot{v} = -\gamma v$$

$$\dot{v} = -\frac{v}{m/\gamma}$$

víz molekulák tipikus megállási ideje:

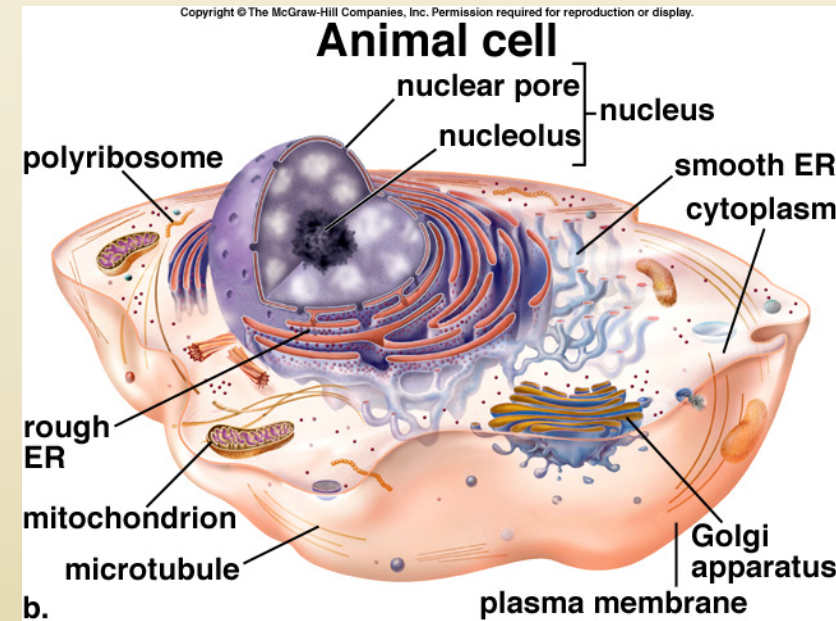
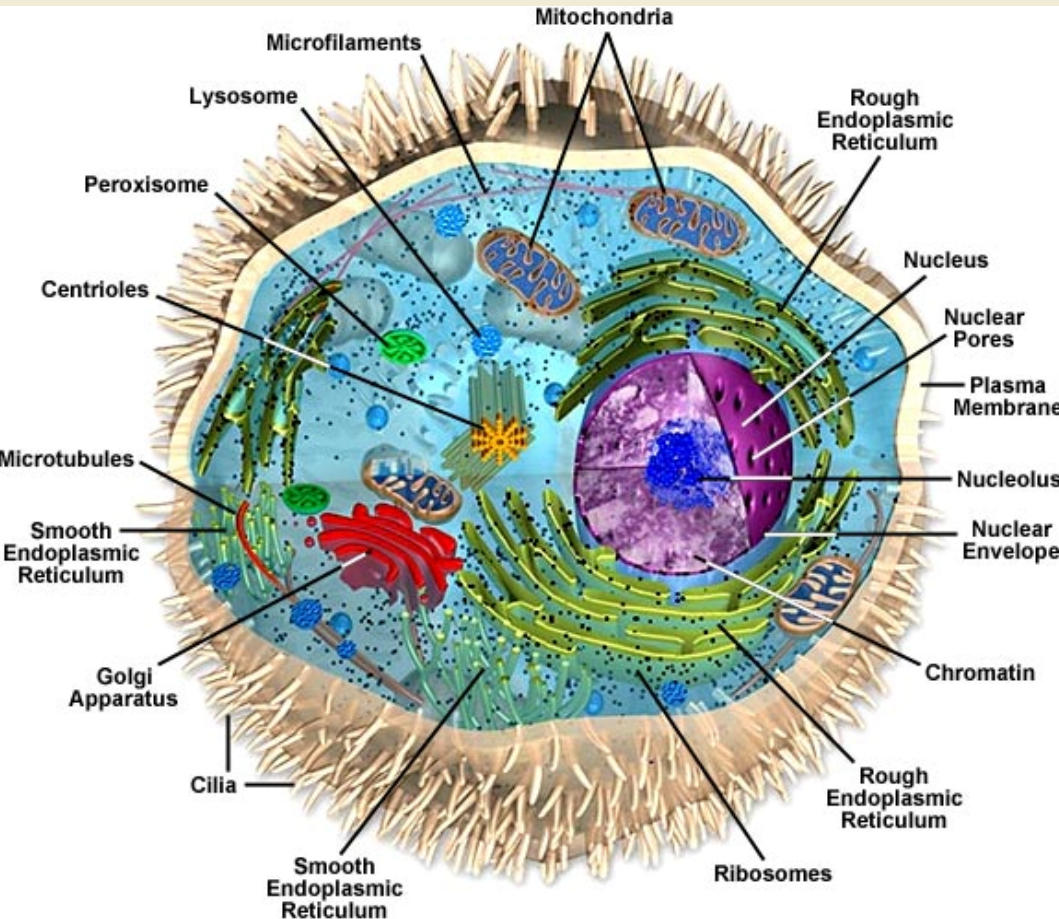
$$\tau = \frac{m}{\gamma} = \frac{m}{6\pi\eta R} = \frac{18 \times 10^{-3} \text{ kg} / 6 \times 10^{23}}{6\pi \cdot 10^{-3} \text{ kg/sm} \cdot 1.5 \times 10^{-10} \text{ m}} \approx 10^{-14} \text{ s}$$

víz molekulák tipikus megállási úthossza:

$$\lambda = v\tau \approx 350 \frac{\text{m}}{\text{s}} \cdot 10^{-14} \text{ s} = 3.5 \times 10^{-12} \text{ m}$$



# Az eukarióta sejtek felépítése



sejtek:  $\sim 10 \mu\text{m}$

sejtszervecskék:  $\sim 1 \mu\text{m}$

biomolekulák:  $\sim 1-10 \text{ nm}$

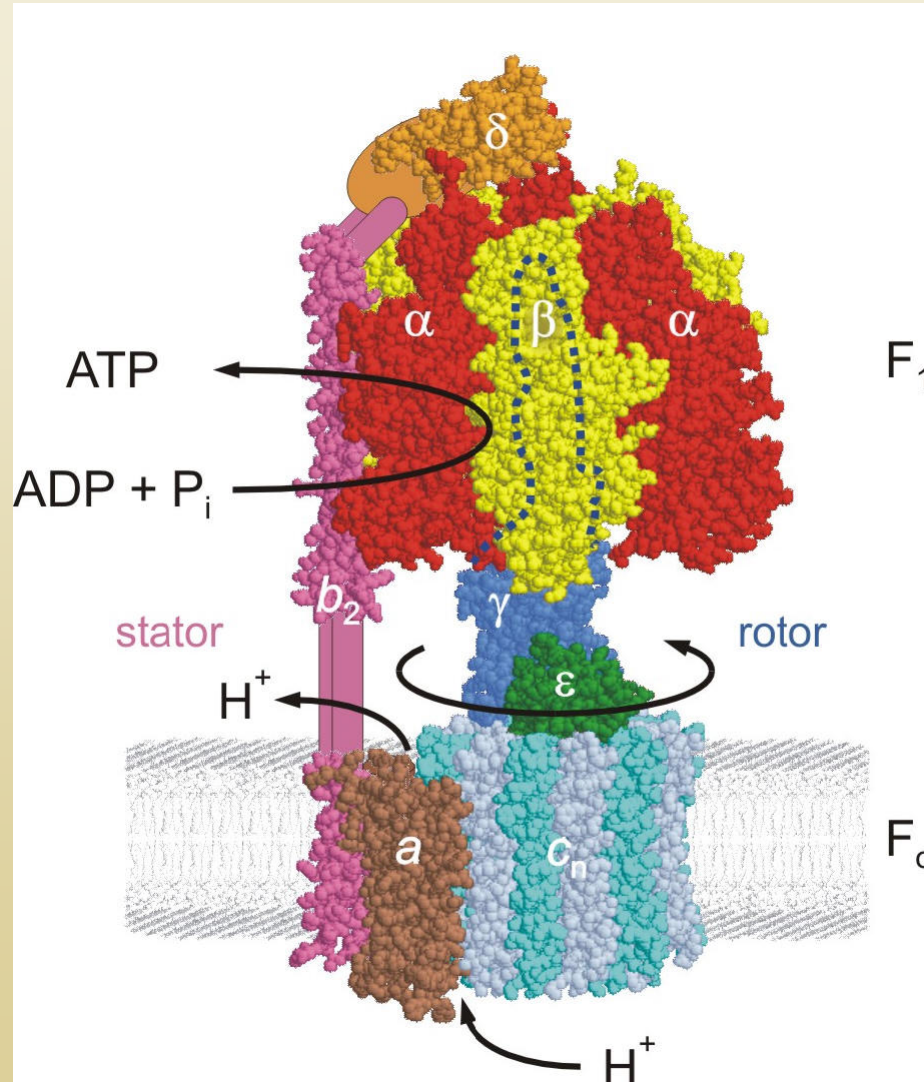
atomok:  $\sim 0.2-0.4 \text{ nm}$

hőmérsékleti energia ( $k_B T$ ):  $\sim 4 \text{ pNnm}$

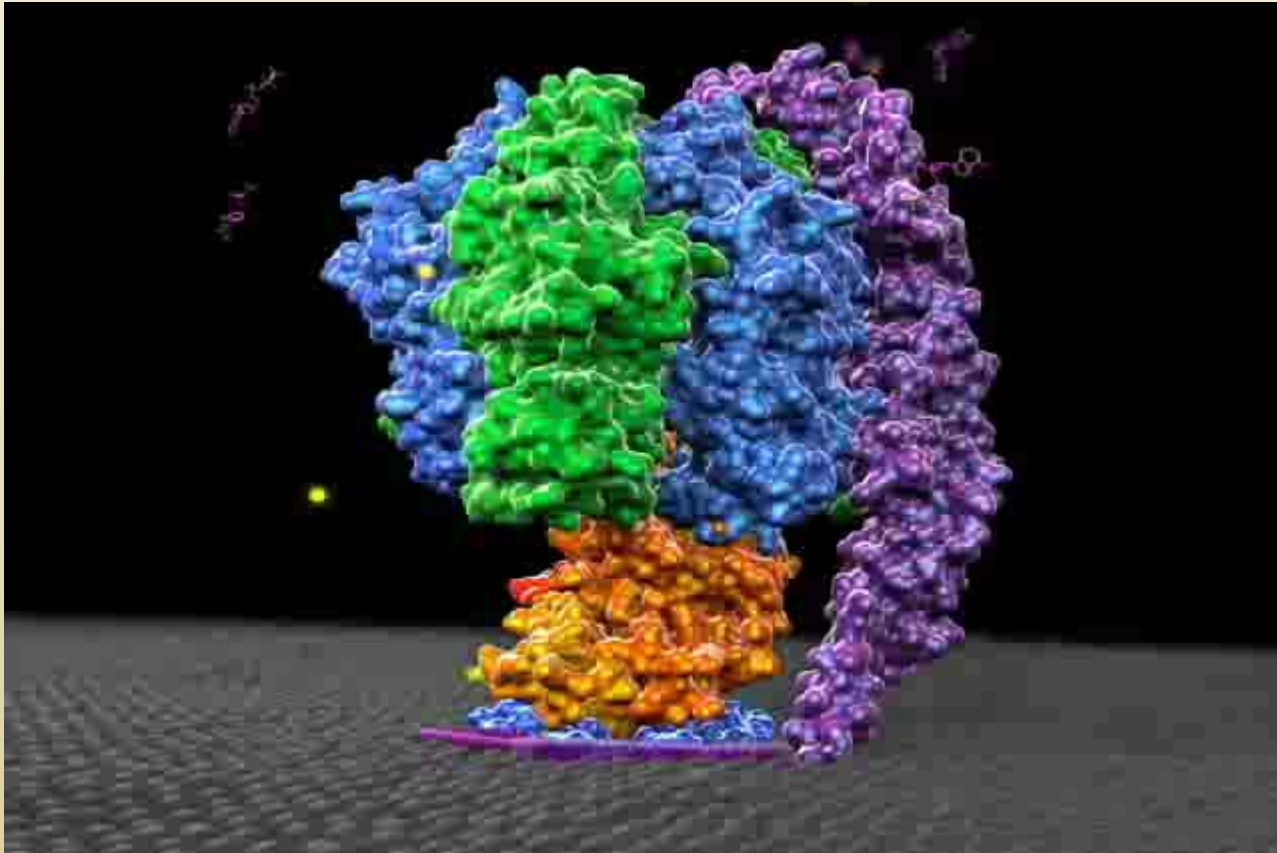
ATP szabadenergia:  $\sim 100 \text{ pNnm}$

tipikus erők:  $\sim 1-10 \text{ pN}$

# Forgó motorfehérjék I: (ATP-szintáz)

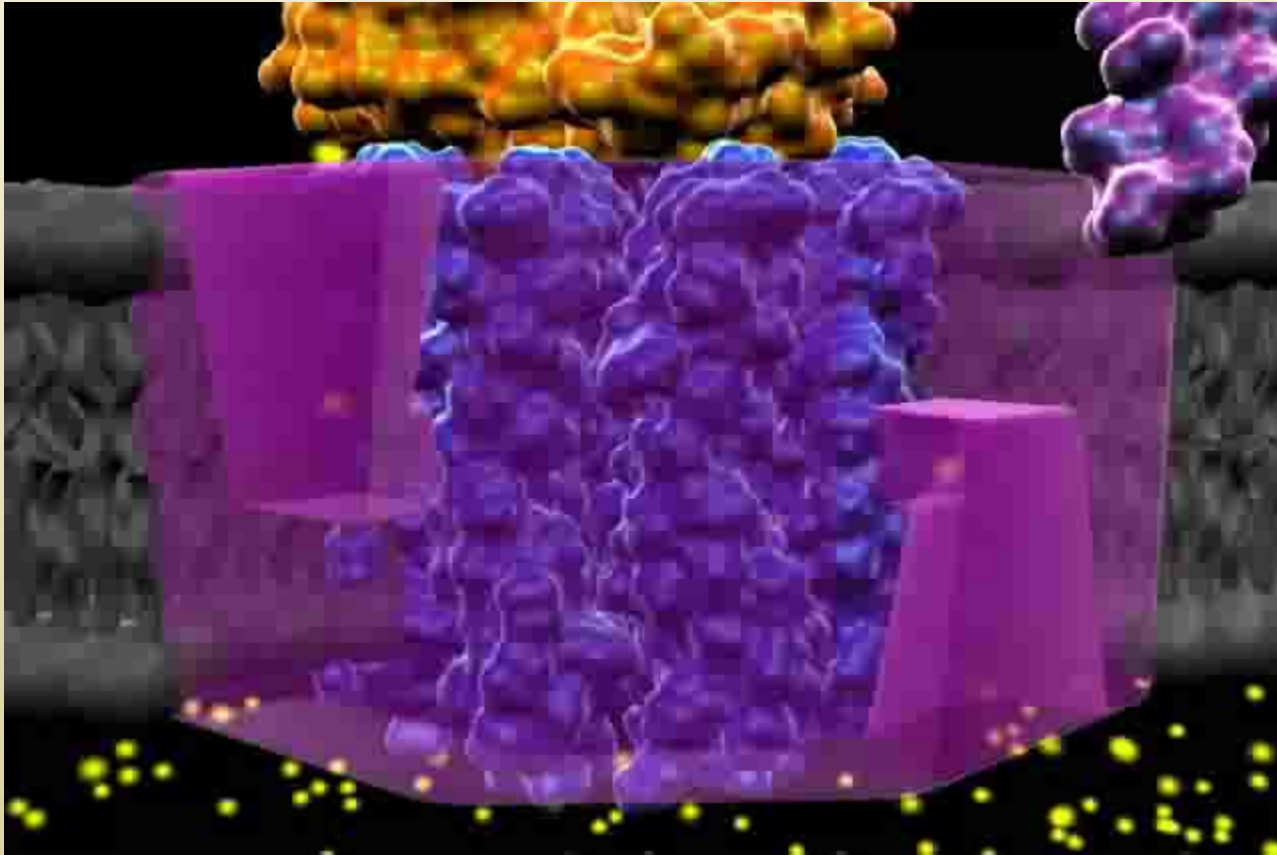


# Forgó motorfehérjék I: (ATP-szintáz)

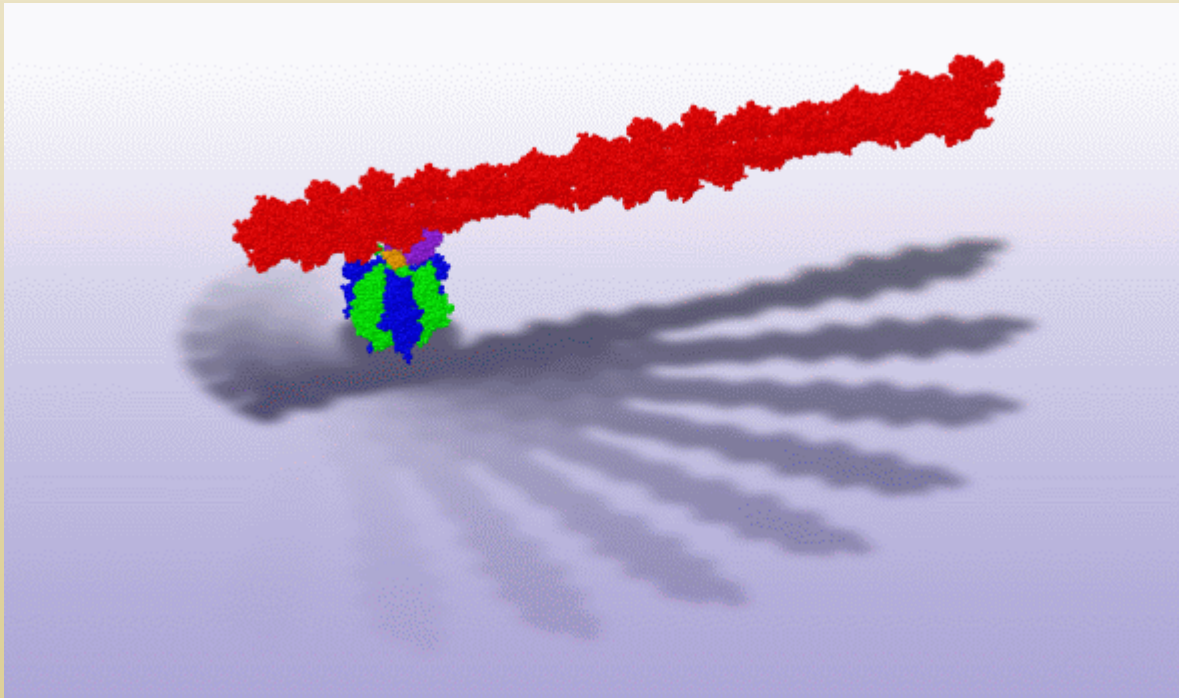
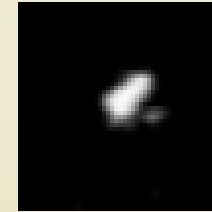




# Forgó motorfehérjék I: (ATP-szintáz)

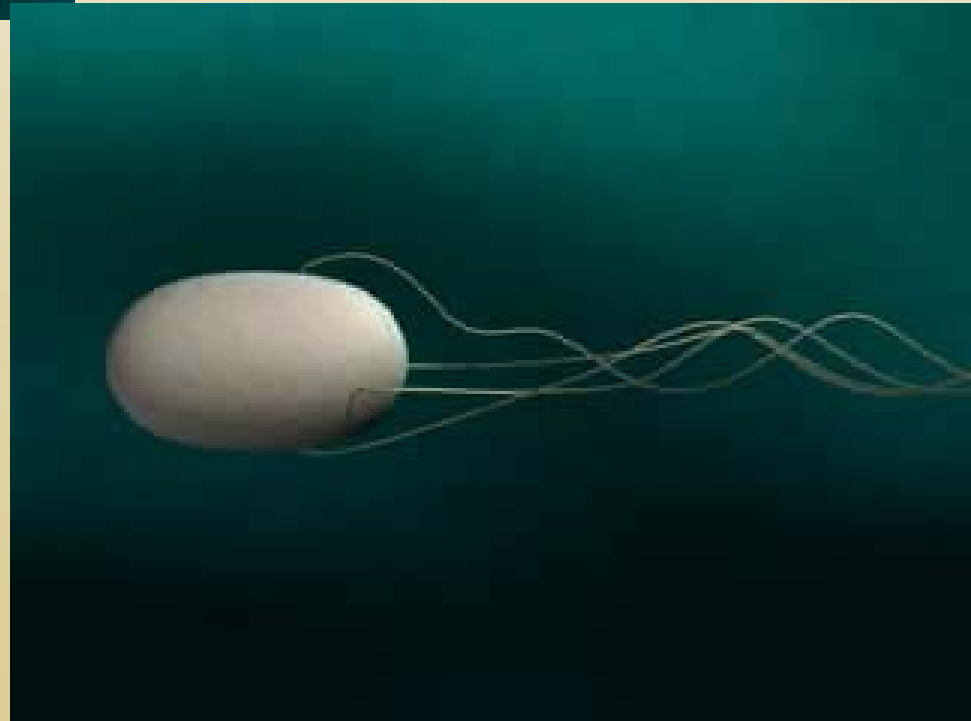
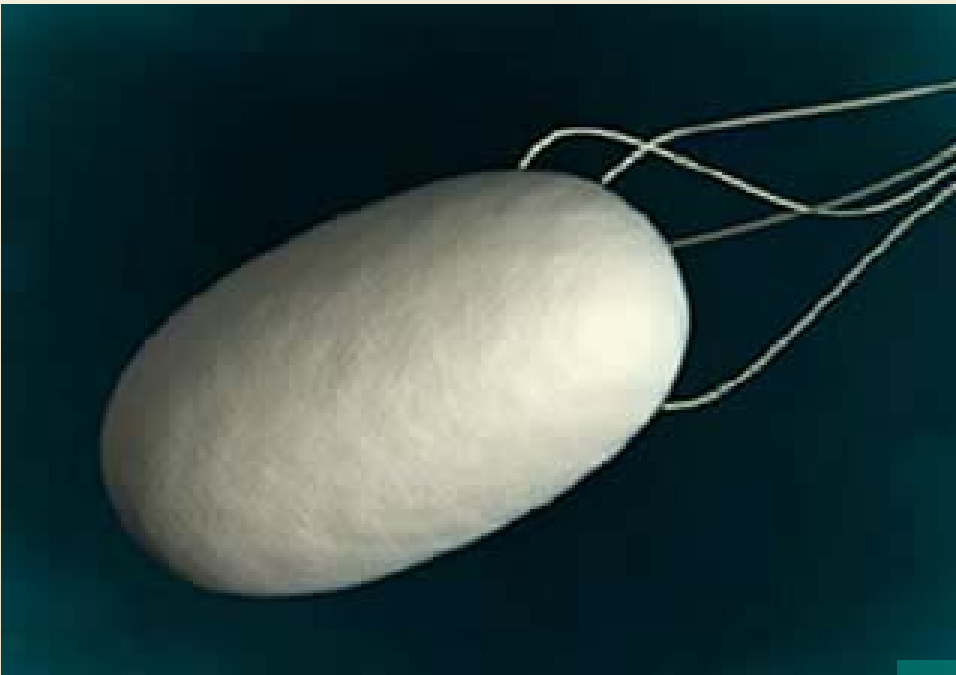


# Forgó motorfehérjék I: (ATP-szintáz)



[K. Kinoshita (1997)]

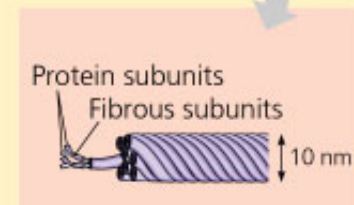
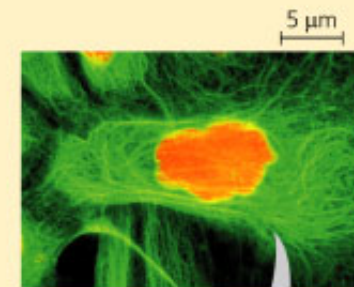
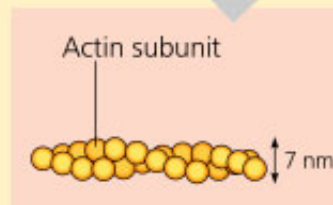
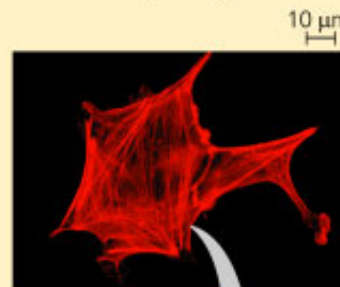
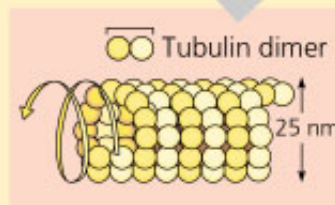
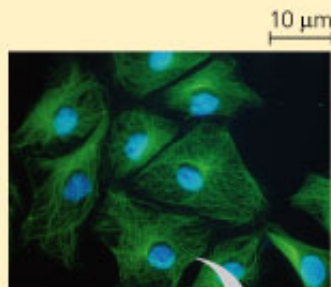
# Forgó motorfehérjék II: (bakteriális flagelláris motor)



# Sejtváz

**Table 7.2 The Structure and Function of the Cytoskeleton**

Property	Microtubules	Microfilaments (Actin Filaments)	Intermediate Filaments
Structure	Hollow tubes; wall consists of 13 columns of tubulin molecules	Two intertwined strands of actin	Fibrous proteins supercoiled into thicker cables
Diameter	25 nm with 15-nm lumen	7 nm	8–12 nm
Protein subunits	Tubulin, consisting of $\alpha$ -tubulin and $\beta$ -tubulin	Actin	One of several different proteins of the keratin family, depending on cell type
Main functions	Maintenance of cell shape (compression-resisting “girders”) Cell motility (as in cilia or flagella) Chromosome movements in cell division Organelle movements	Maintenance of cell shape (tension-bearing elements) Changes in cell shape Muscle contraction Cytoplasmic streaming Cell motility (as in pseudopodia) Cell division (cleavage furrow formation)	Maintenance of cell shape (tension-bearing elements) Anchorage of nucleus and certain other organelles Formation of nuclear lamina

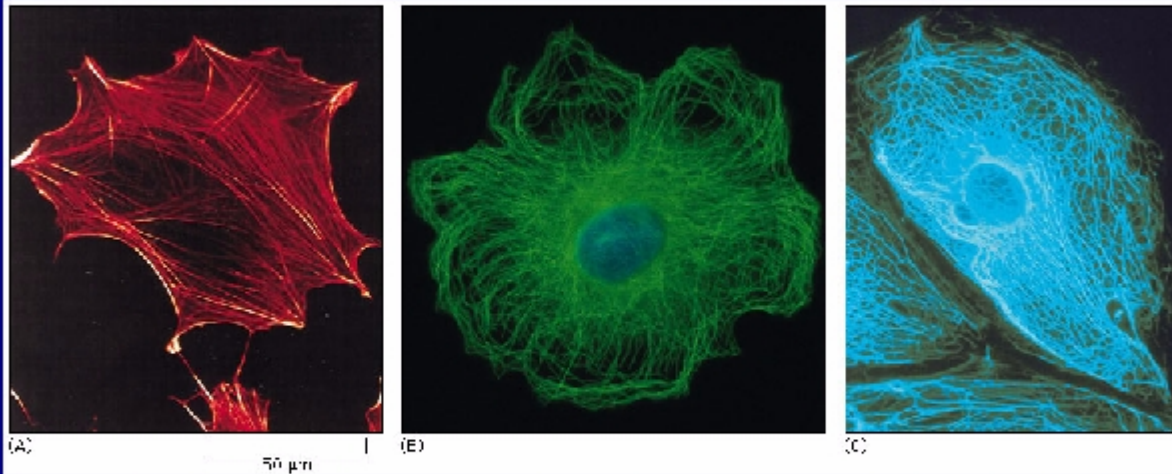


SOURCE: Adapted from W. M. Becker, L. J. Kleinsmith, and J. Hardin, *The World of the Cell*, 4th ed. (San Francisco, CA: Benjamin Cummings, 2000), p. 753.



# Sejtváz

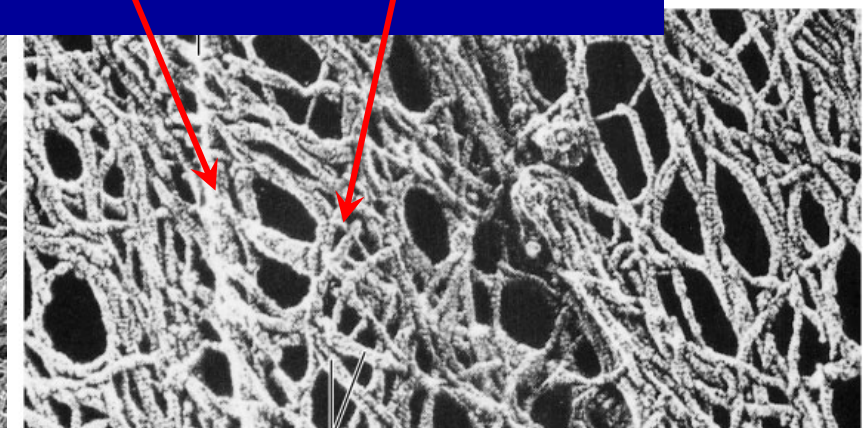
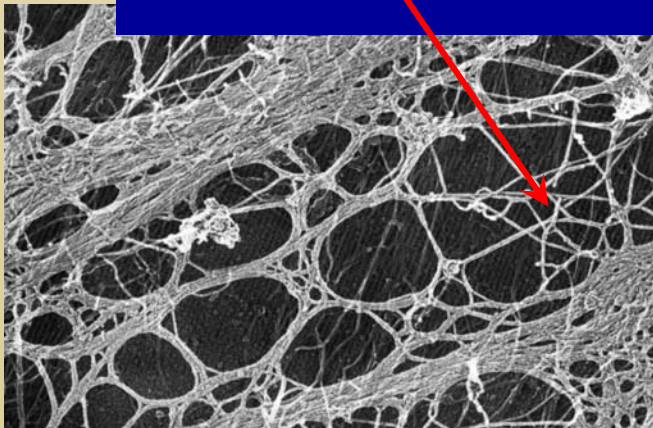
## Cytoskeleton



Actin Filaments

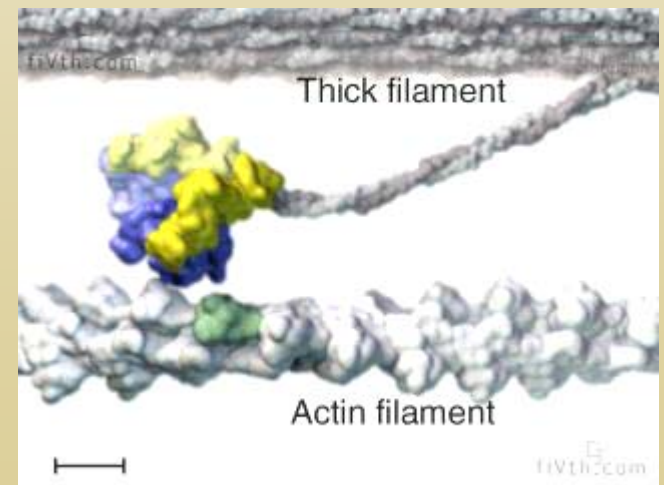
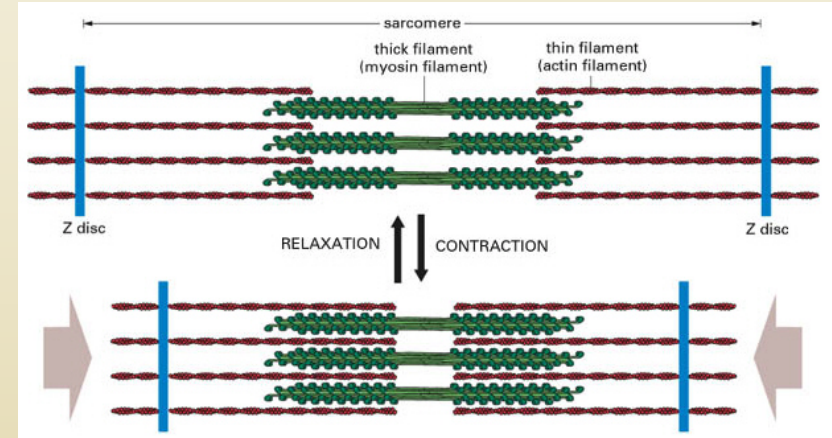
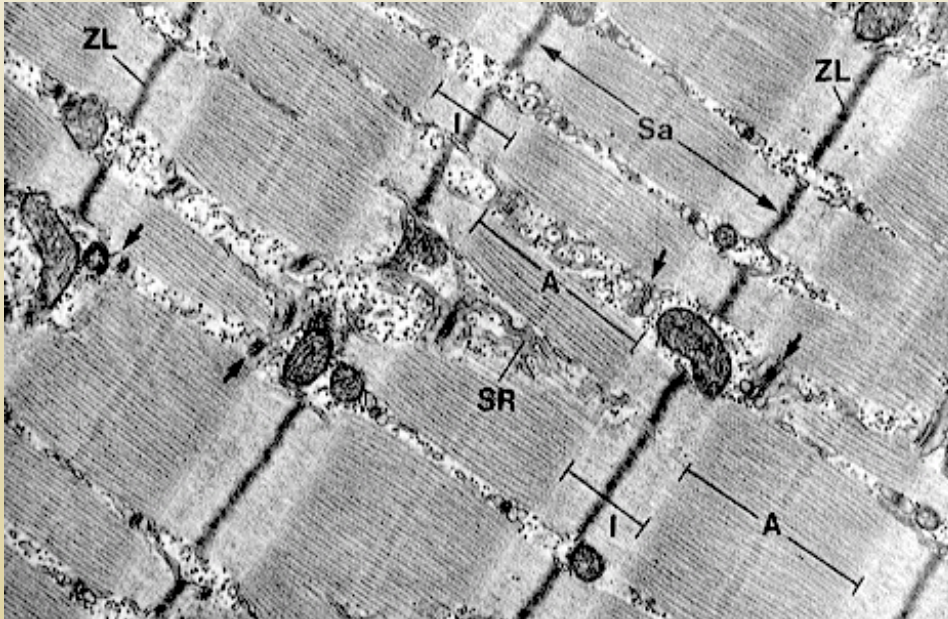
Microtubules

Intermediate  
Filaments

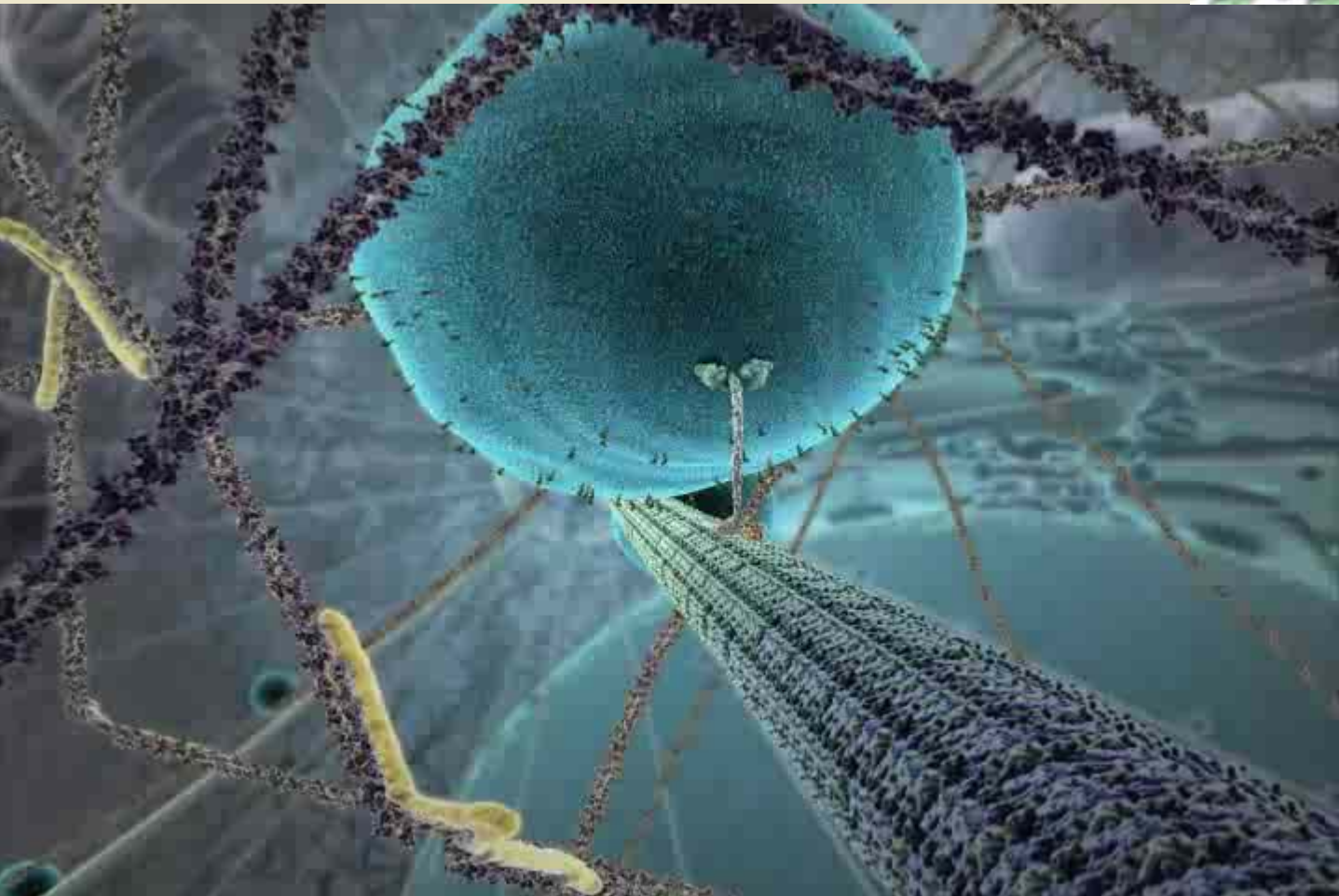
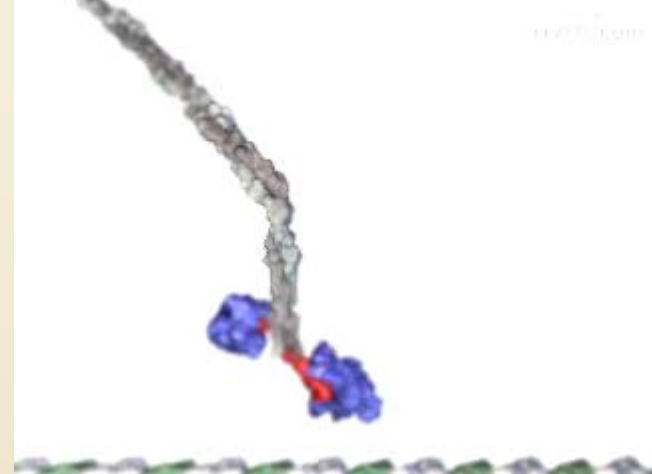




# Lineáris motorfehérjék I: (miozin aktin szál mentén)



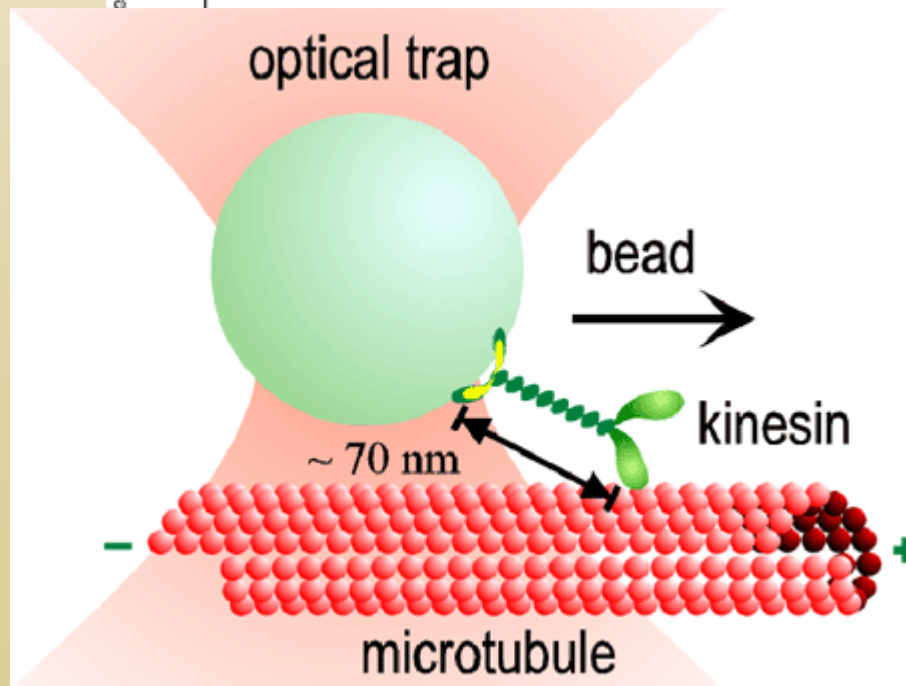
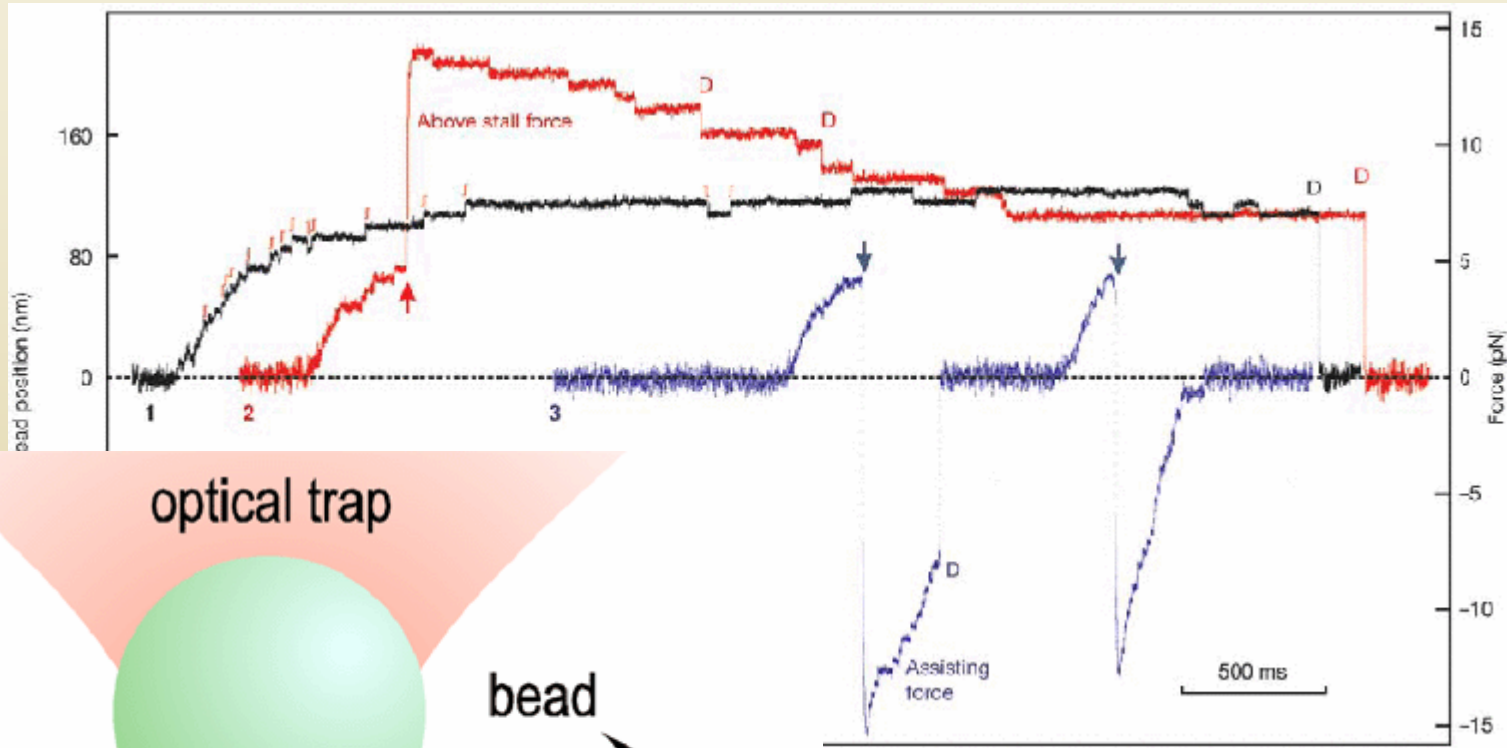
# Lineáris motorfehérjék II: (kinezin mikrotubulus mentén)



[R.Vale]

[Harvard Univ.:  
The inner life of the cell]

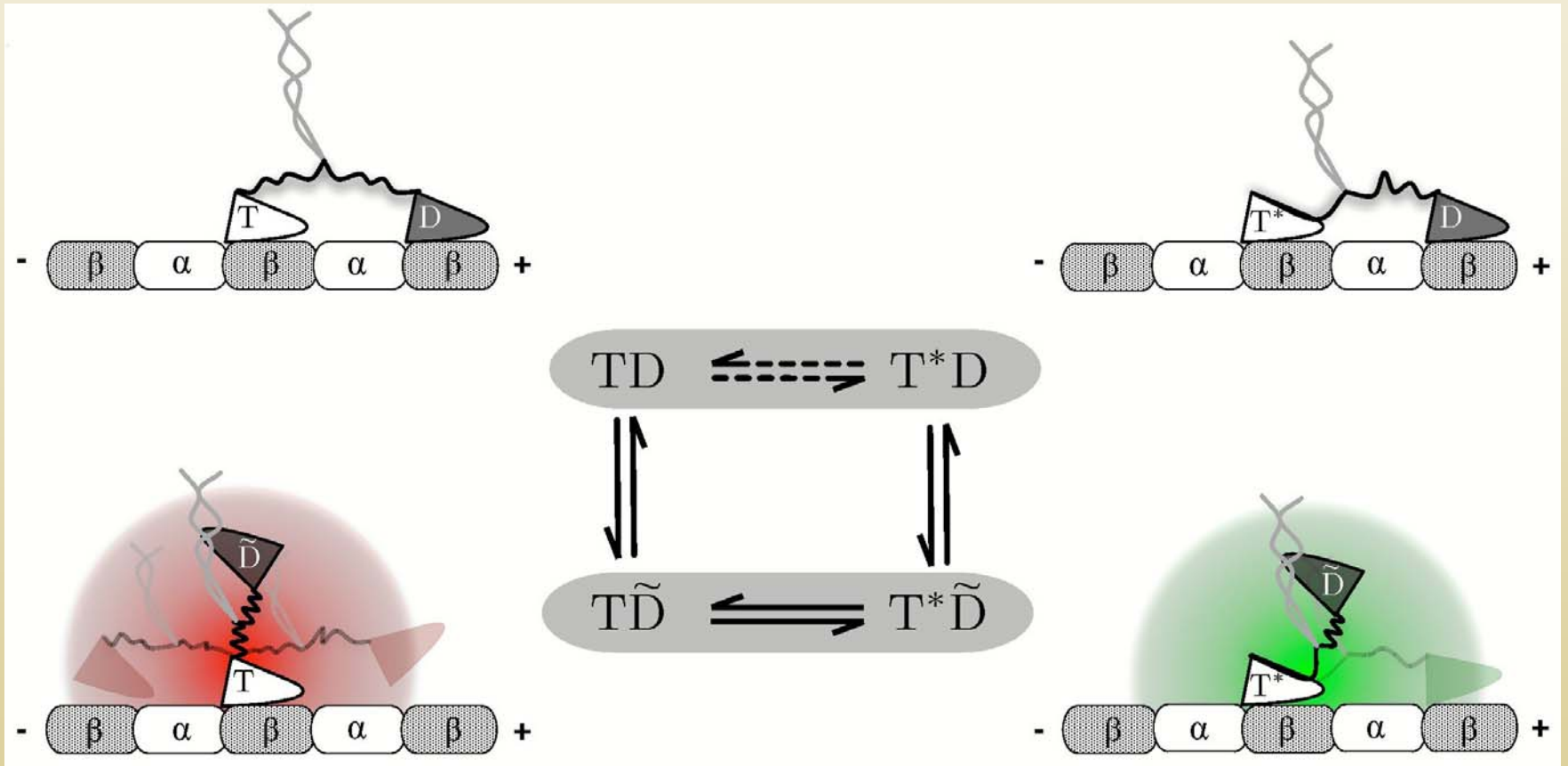
# Optikai csipesz



[Carter and Cross, Nature **435**, 308 (2005)]



# Kinezin modell



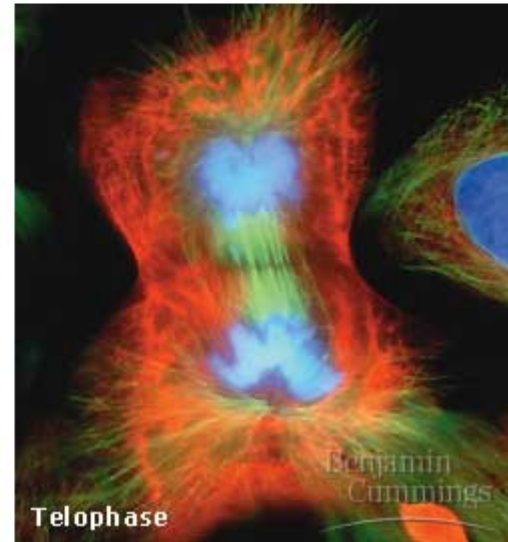
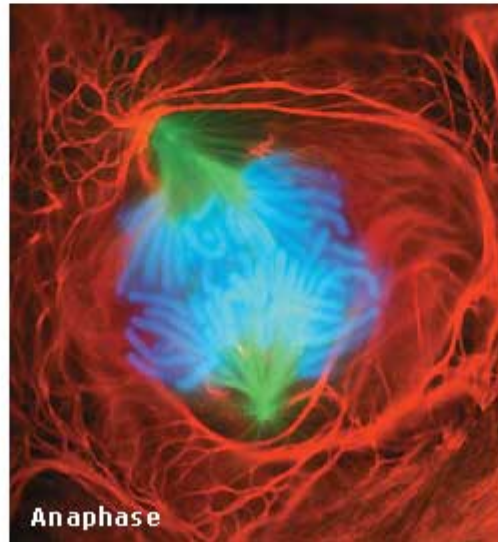
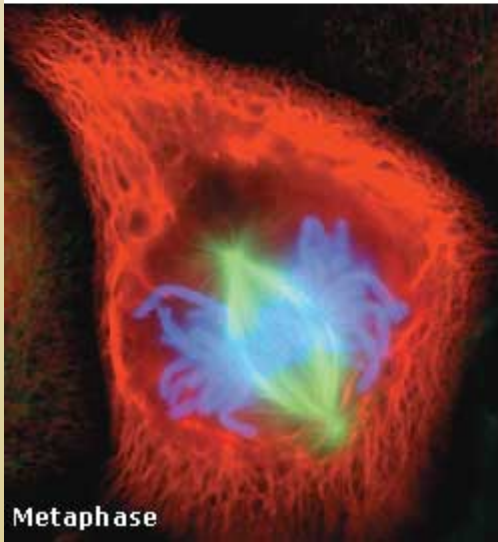
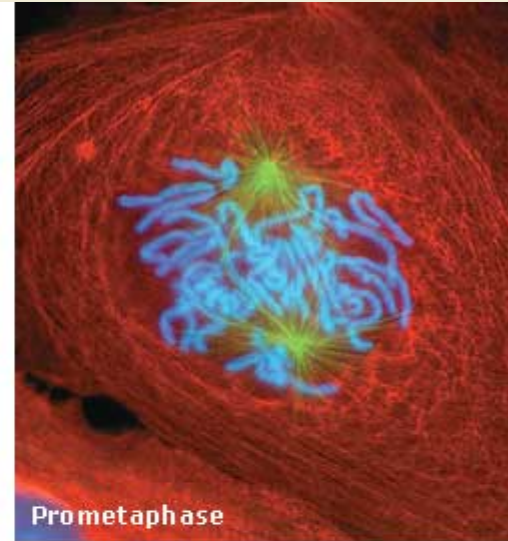
# diffúzió --- motor transzport

diffúziós együttható:  $D \approx 10^{-10} \frac{\text{m}^2}{\text{s}}$   $l^2 \approx Dt$

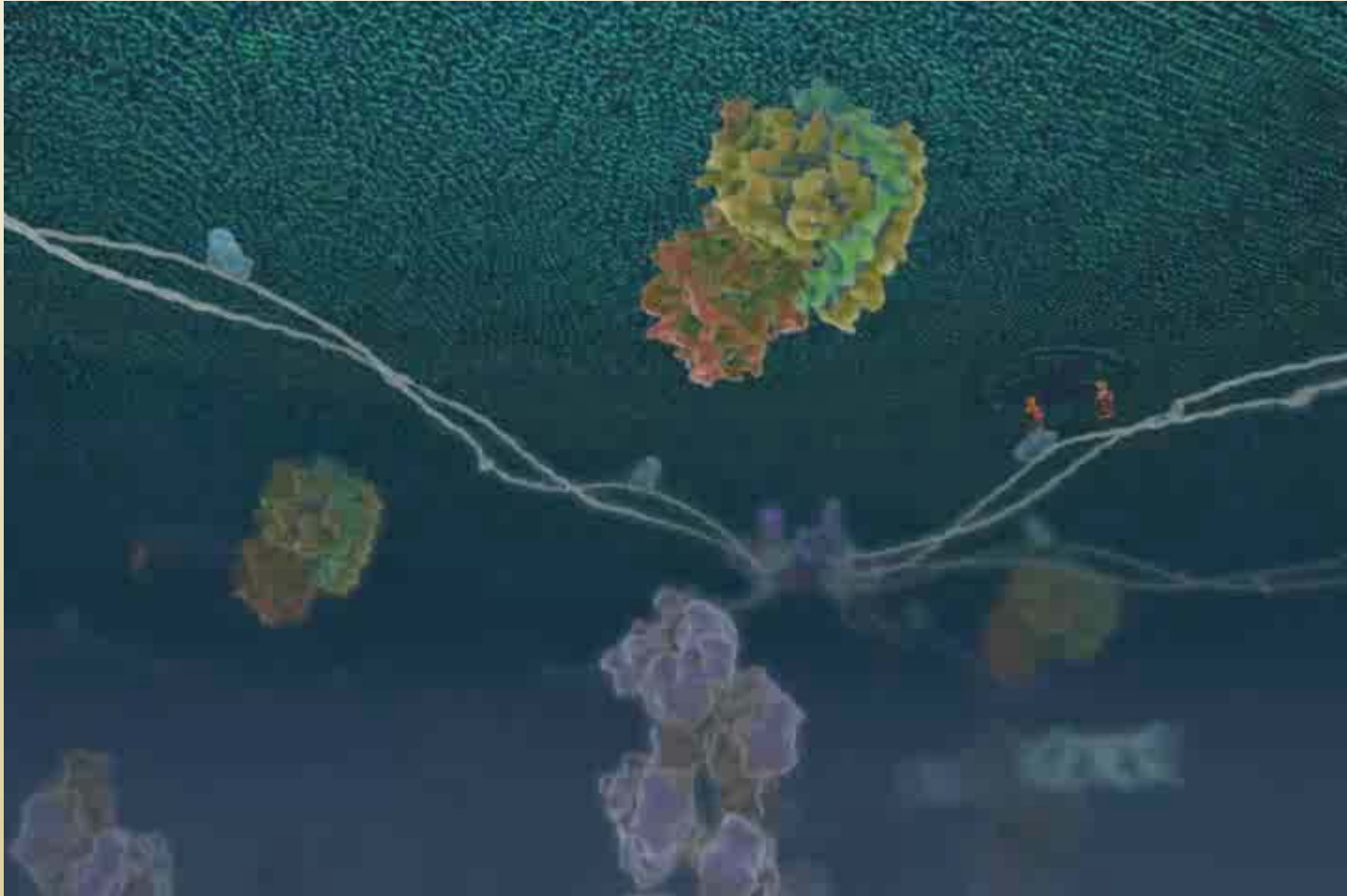
$$t \approx \frac{l^2}{D} \begin{cases} \frac{(10 \times 10^{-6} \text{ m})^2}{10^{-10} \text{ m}^2/\text{s}} = 1 \text{ s} \\ \frac{(1 \text{ m})^2}{10^{-10} \text{ m}^2/\text{s}} = 10^{10} \text{ s} \approx 300 \text{ y} \end{cases}$$

$$t \approx \frac{l}{v} \begin{cases} \frac{10 \times 10^{-6} \text{ m}}{10^{-6} \text{ m/s}} = 10 \text{ s} \\ \frac{1 \text{ m}}{10^{-6} \text{ m/s}} = 10^6 \text{ s} \approx 12 \text{ d} \end{cases}$$

# Sejtosztódás

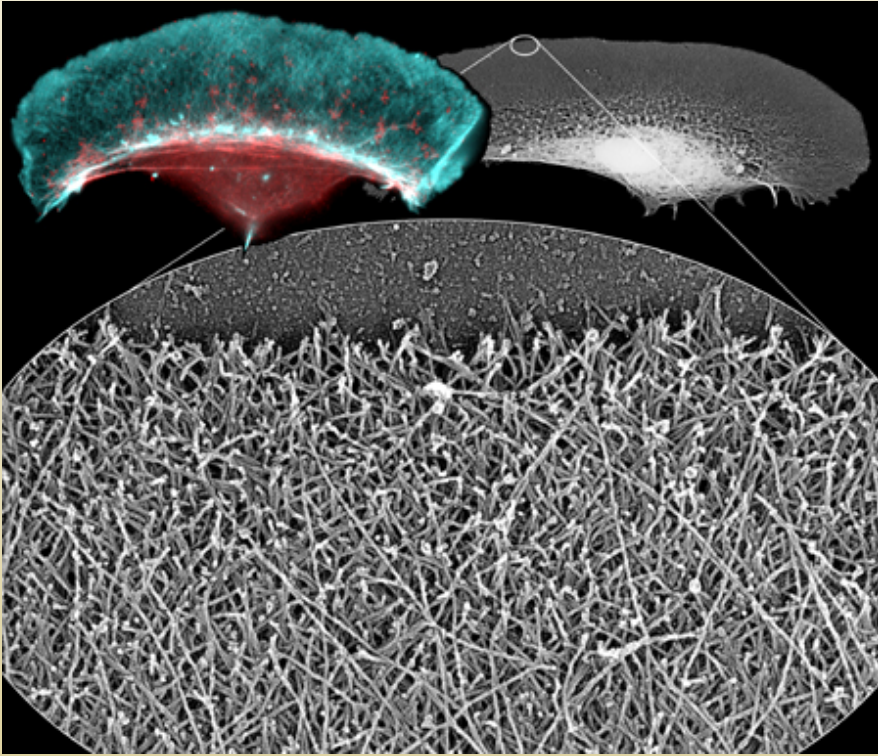


# Aktin és mikrotubulus polimerizáció



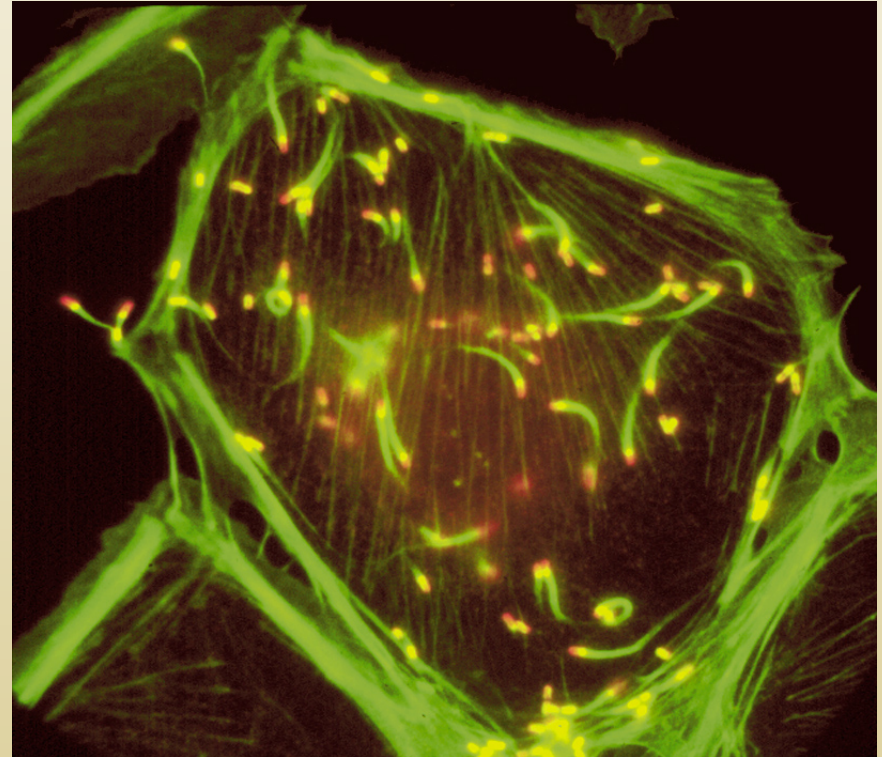


# Mozgás aktinpolimerizációval



**Lamellipodium**

[G. Borisy, Northwestern Univ.]

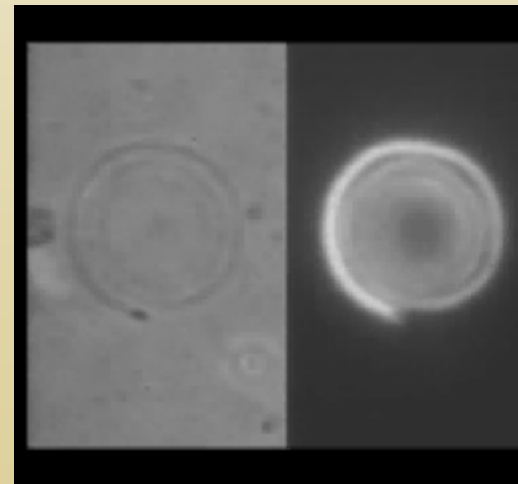
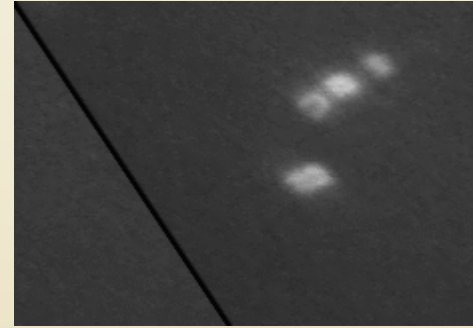
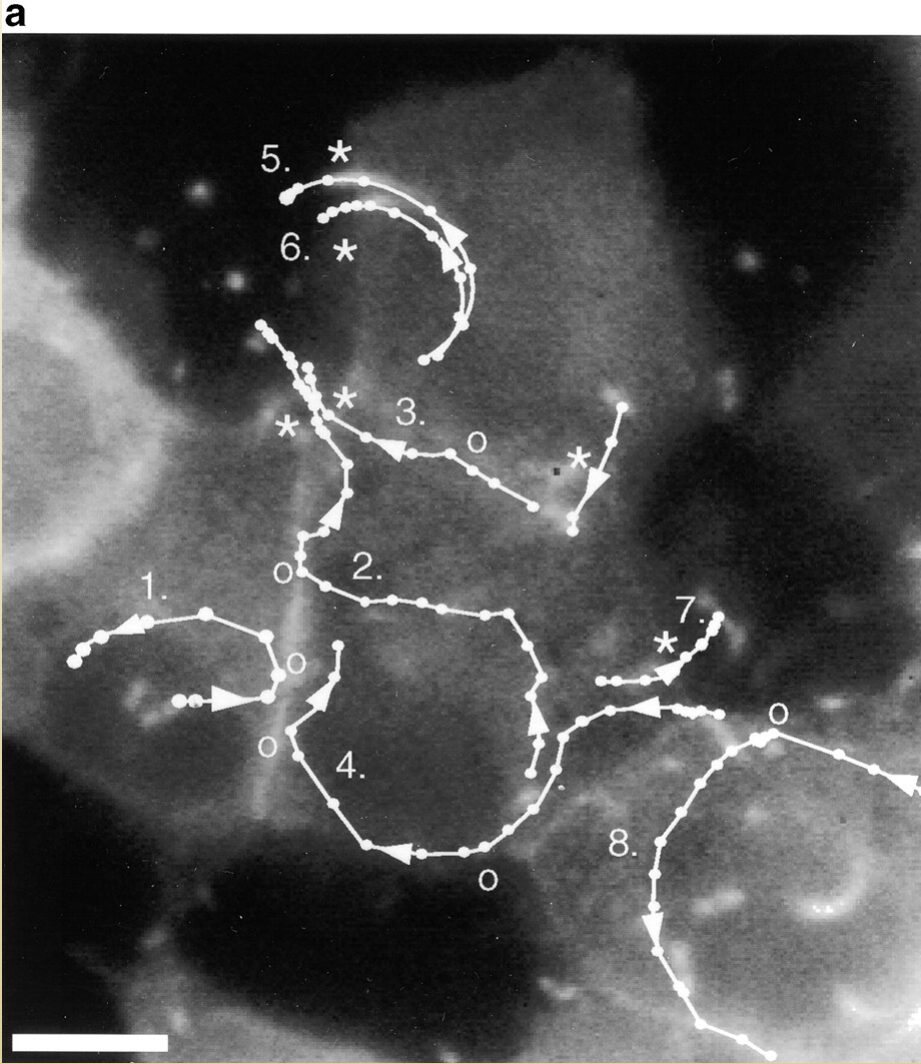


**Listeria**

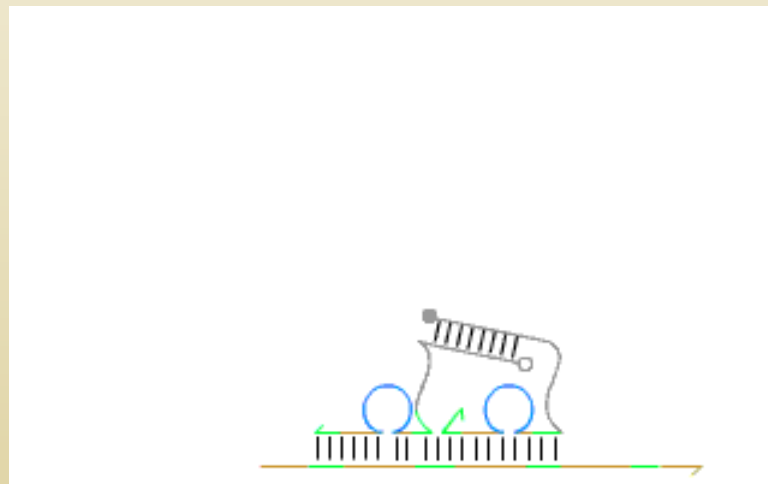
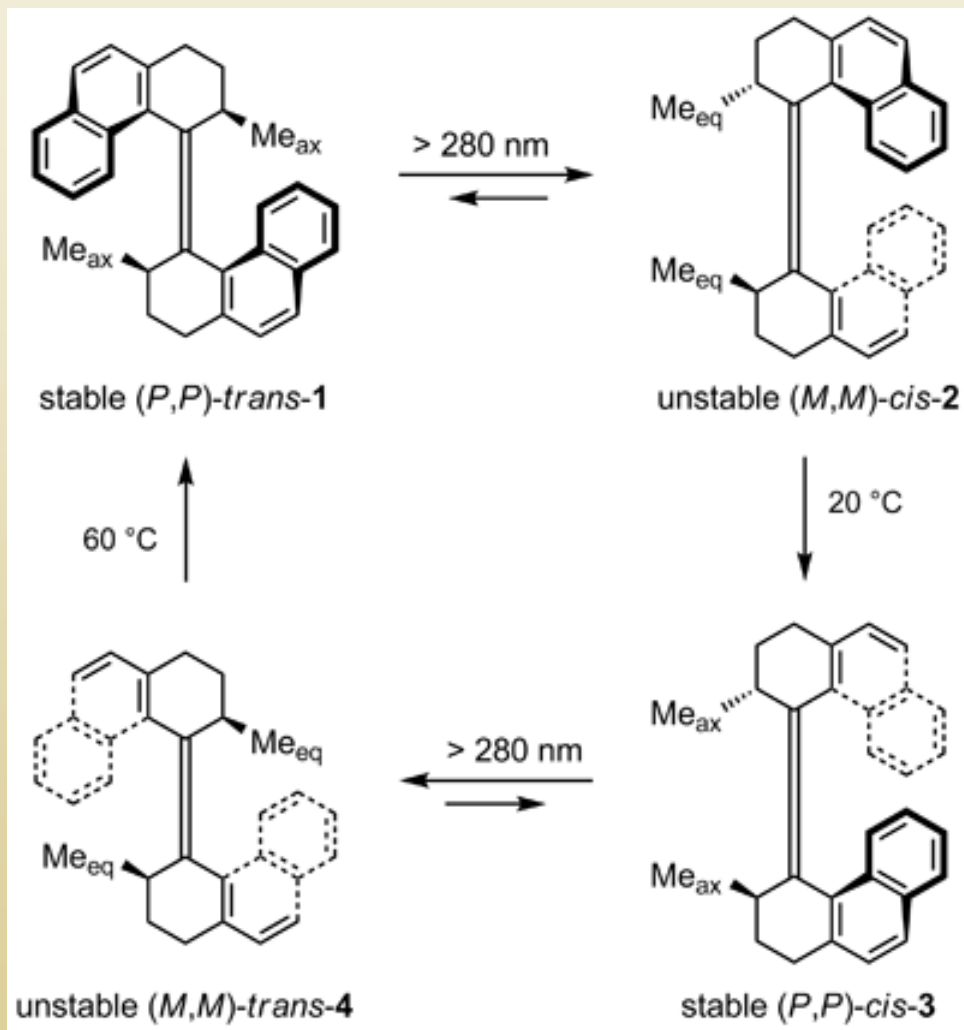
[J. Theriot, Stanford Univ.]



# Listeria



# Szintetikus motorok:



[Andrew Turberfield]

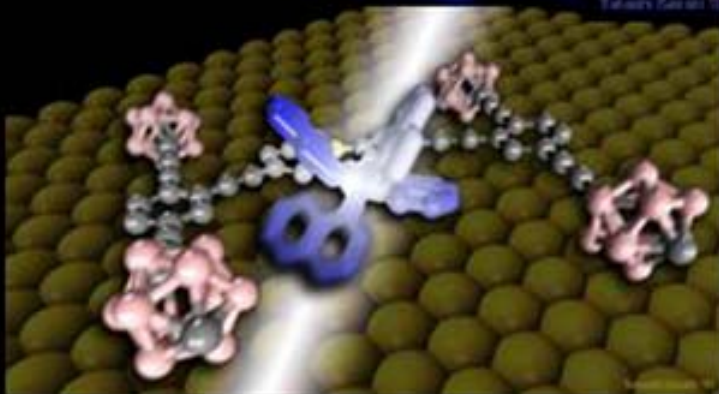
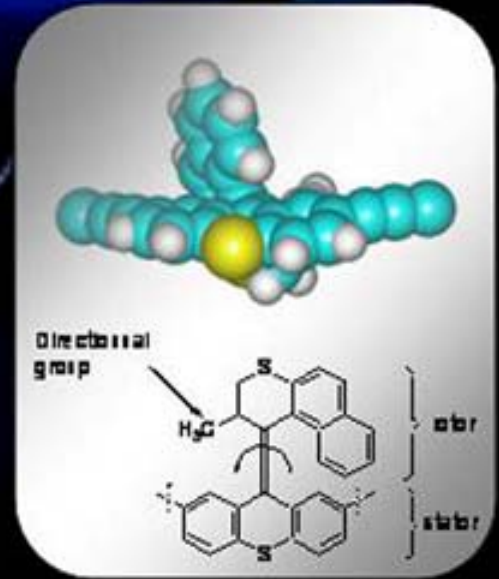
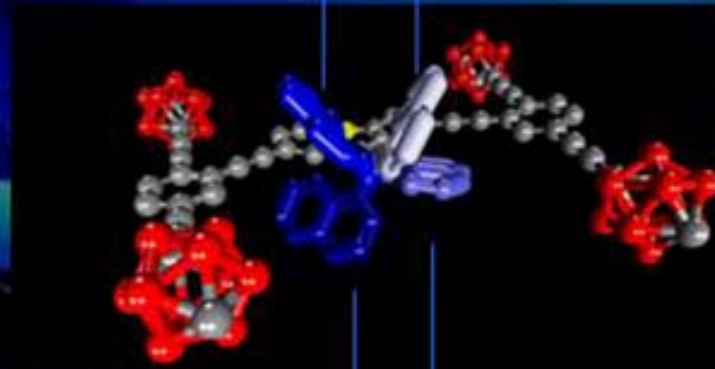
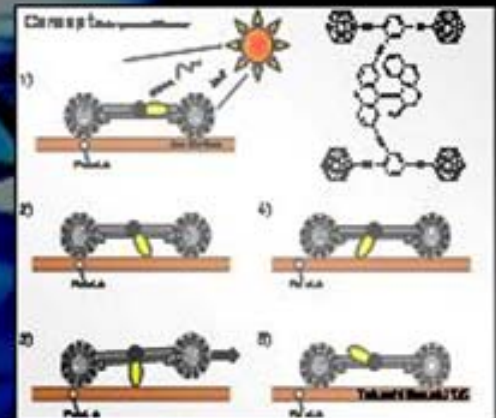
[Ben Feringa]

# Motorized Nanocar



Solar-Powered Engine

Concept



The Engine

Rolling on Surface:  
(concept illustration)